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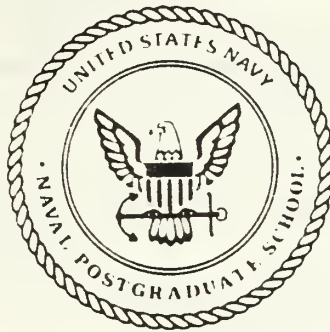
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THESIS

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EFFECTS OF CHARGE DISTRIBUTION
WITHIN A PARTICLE BEAM
ON THE SUB-CERENKOV RADIATION

by

Jung, Yun Su
December 1987

Thesis Advisor:

John R. Neighbours

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Effects of Charge Distribution within a Particle Beam
on the sub-Cerenkov Radiation

by

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B.S., Republic of Korea Military Academy, 1974

Submitted in partial fulfillment of the
requirements for the degree of

MASTER OF SCIENCE IN PHYSICS

from the

NAVAL POSTGRADUATE SCHOOL
December 1987

ABSTRACT

The charge distribution of periodic electron beam pulses generates patterns of sub-Cerenkov radiation distinctive of the distribution of charge within a bunch. Mapping the radiation pattern from different charge shapes may provide insight into whether charge pulse shapes can be determined from observed radiation patterns. The radiation patterns of Gaussian, Level, and Trapezoidal function were mapped by computer simulation. Near 90° to the beam, the radiation patterns of all three charge distributions developed an envelope proportional to the Fourier transform of the charge bunch distribution when the wavelength of the emitted radiation was comparable to the size of the bunch. For the Gaussian function, the envelope is Gaussian, for the level function it is a sinc function. Since the envelope for the trapezoidal function is the product of two sinc functions it is more difficult to analyze. This work may provide a basis for determining the charge shape of electron beam pulses from the sub-Cerenkov radiation based on the radiation intensity pattern.

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I. INTRODUCTION

A. HISTORY

A very faint emission of bluish-white light, what was later-on called Cerenkov radiation, from transparent substances placed nearby a radioactive sources had been observed by Mme Curie in 1910 . Although electromagnetic theory had been sufficiently developed at that time to describe this phenomenon, the first deliberate attempt to study the phenomenon was made by Mallet after many years, who found that the light emitted from a wide variety of transparent bodies placed close to radioactive source always had the same bluish-white light quality, and that spectrum was continuous, not possessing the line or band structure characteristic of fluorescence [Ref. 1: p. 1].

P.A. Cerenkov carried out a series of experiments between 1934 and 1938 related to the phenomenon. In 1937 Ilya Frank and Igor Tamm proposed a satisfactory theory of the radiation. The experimental results and theoretical predictions were in excellent agreement. A complete description of Cerenkov radiation, as well as exact mathematical treatment is given in [Ref. 1: p. 1].

B. WHAT IS THE CERENKOV RADIATION ?

A charged particle or a group of charged particles moving through a medium at a speed greater than the (phase) velocity of light in the same medium will generate a continuous spectrum of electromagnetic radiation. This process is referred to as Cerenkov radiation.[Ref. 2: p.9]

C. PREVIOUS RESEARCH AT N.P.S.

The research on Cerenkov radiation has been conducted by Professors Fred R. Buskirk, John R. Neighbours and others in the Naval Postgraduate school since the LINAC was established. Recent work has concentrated on the determination of electron beam bunch profile through Cerenkov radiation.

The work was aimed to illustrate examples of the consequences of the finite spatial charge distribution to show that Cerenkov radiation emitted at low microwave frequencies may be used to characterize the properties of an intense relativistic beam in air. The results were that the spatial charge distribution of an electron pulse, along with the beam interaction length, determines the Cerenkov radiation distribution as a function of frequency. An angular distribution of the Cerenkov radiation can, in principle, measure its spatial charge distribution.[Ref. 3:p. 1994].

D. PURPOSE

The charge distribution of a bunch influences the pattern of radiation produced. Detailed calculations for several simple charge distributions have been carried out for the Cerenkov case [Ref. 4:pp. 1994,1996]. The object of this work is to assess the effect of the charge distribution of a bunch on the sub-Cerenkov radiation from a charged particle beam. Specifically, this means investigation of the short beam path region at energies below the threshold.

II. THEORY

A. BACKGROUND

A fast, charged particle may cause electromagnetic radiation in a dielectric medium when it moves with a constant speed. Suppose an electron to be moving relatively slowly through a transparent medium as shown on Fig.1.1 a). As the particle passes through the medium, each elemental region of the medium along the track will in turn receive a very brief electromagnetic pulse and be polarized, producing a dipole. An electromagnetic pulse is generated by the formation and disappearance of the dipole as the bunch passes. The electromagnetic pulse propagates away from the dipole source at the velocity of light in the medium. The distance between wave fronts is compressed as the velocity of the electron bunch increases. This effect is similar to the doppler effect for sound radiated from a moving source. If the speed of the particle is less than the propagation velocity in the medium, the electromagnetic field produced is called sub-Cerenkov radiation. [Ref. 1: pp. 3-4]

If the electron is moving faster than light in the medium (see Fig 1.1 b), the the pulse source velocity is greater than that of the propagating electromagnetic wave which transport the energy. The result is a wavefront and where the emanated wavelets bunch together in phase. This shockfront of electromagnetic radiation is Cerenkov radiation. [Ref. 1: pp. 4-5]

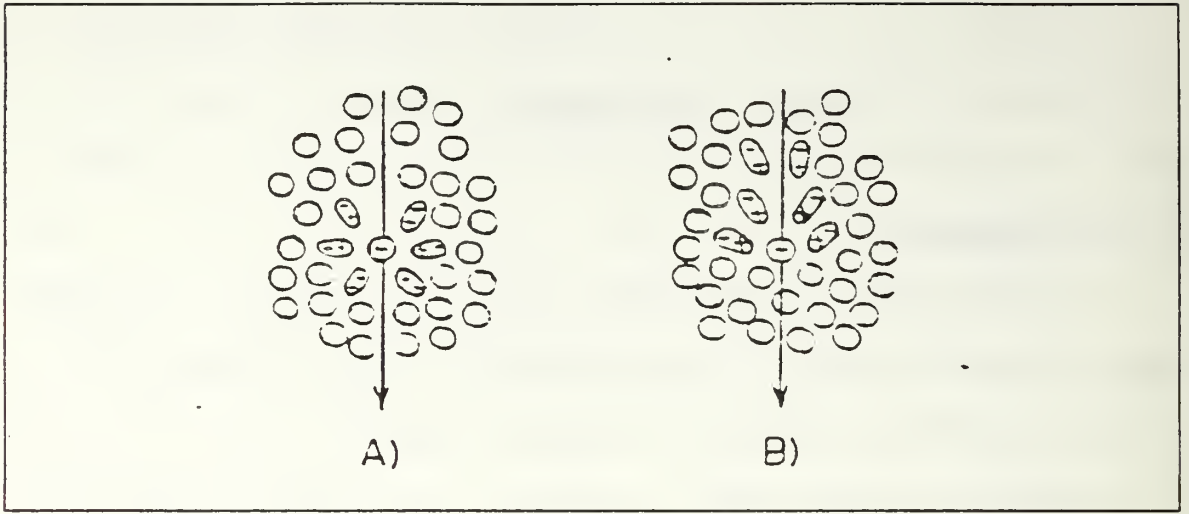


Fig. 2.1 Polarized Atoms in a Dielectric.

B. CHARACTERISTICS OF CERENKOV RADIATION

Fig. 2.2 shows the resultant Cerenkov radiation plane wavefront BC from particles traveling from A to B. Wavelets from point 0 to 5 are coherent along wavefront BC. The angle θ_c is given by the "Cerenkov relation":

$$\cos \theta_c = 1 / \beta n, \quad (2.1)$$

where n is the refractive index of the medium and β is the ratio of the velocity of the particle to the velocity of light in a vacuum [Ref. 1: pp.4-5].

From the above, the following is seen that:

- (1) For medium of given refractive index n , there is a threshold velocity $\beta_{\min} = (1/n)$, below which no radiation take place [Ref. 1: p. 5].
- (2) For ultra-relativistic particles, for which $\beta \cong 1$, there is a maximum angle of emission, given by $\theta_{\max} = \cos^{-1}(1/n)$.
- (3) Radiation occurs mainly in the visible and near visible region for

which $n > 1$. In the X-ray region, above atomic resonances, n is usually less than 1; therefore Cerenkov radiation in the X-ray region is not probable [Ref. 3: p. 3252, Ref. 1: p. 6].

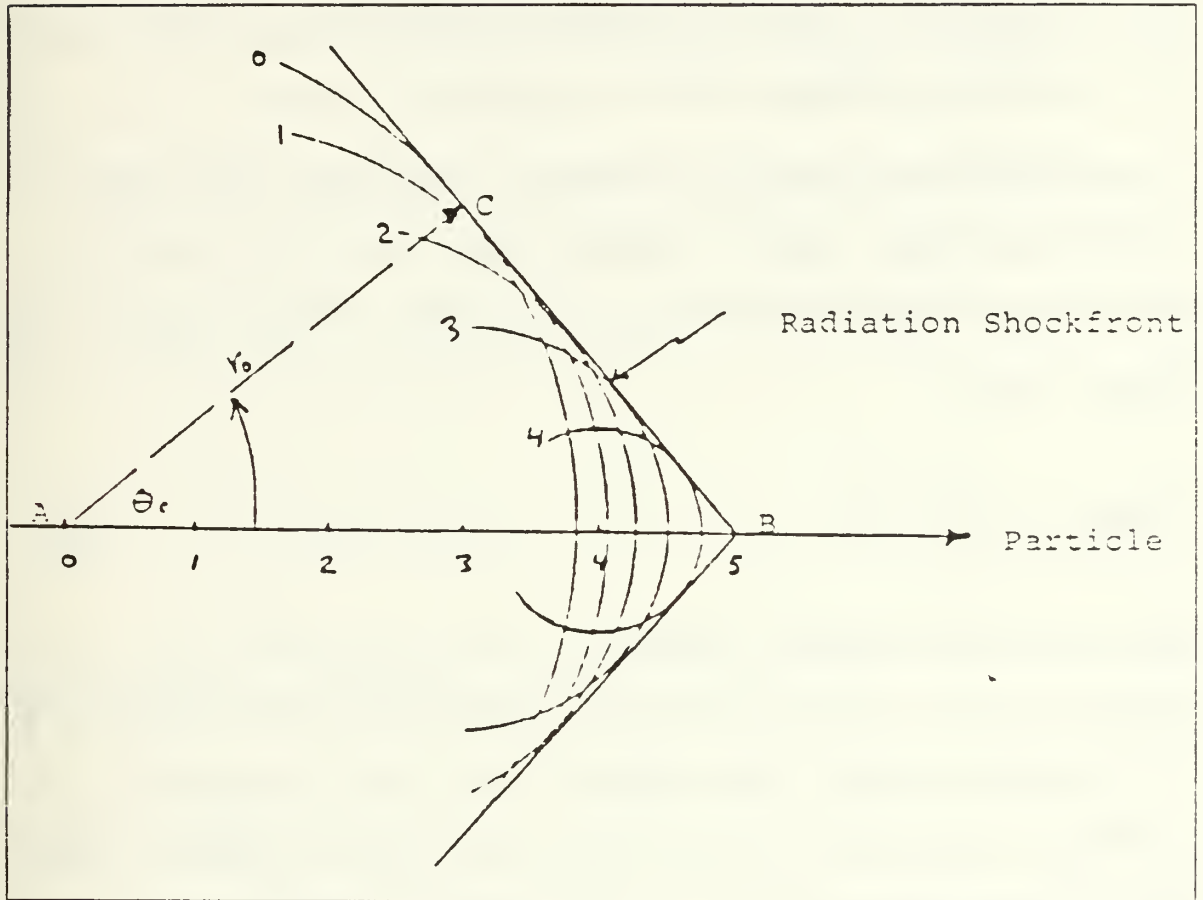


Fig. 2.2 Radiation Shockfront

- (4) In a gas, θ_c has only a slight dependence on electron velocity because β must be close to one in order to obtain the Cerenkov condition [Ref. 3: p. 3249].

From the nature of the radiation, which has been described above, it may be

concluded:

- (5) Azimuthal symmetry of the radiation produces a cone of radiation.
- (6) The distribution in θ of the radiation intensity approximate a Dirac δ -function centered about Cerenkov angle ' θ_c '.
- (7) Length AB in Fig.2 must be much larger than the radiated wavelength in order to avoid diffraction effects. For a finite radiation length, the diffraction effect is significant.

C. CALCULATED POWER OF COHERENT CERENKOV RADIATION

The total coherent power per unit solid angle, radiated at the frequency ν by a periodic charged particle beam in traveling a finite distance L at constant velocity is

$$W(\nu, k) = \nu_0^2 Q R^2, \quad (2.2)$$

where ν_0 is the fundamental frequency of the beam generator and ν is a harmonic of ν_0 , q is the charge of an individual bunch, Q is a constant and R is the radiation function. The bunches in the beam are assumed to be unchanging in shape and size as the beam travels through the medium (usually air) at a velocity given by $\nu = \beta c_0$. The velocity of light in vacuum is c_0 and the velocity of light in the medium is $c = c_0/n$ where n is the index of refraction. The parameters used to describe the radiation are

$$Q = \mu c q^2 / 8 \pi^2, \quad (2.3)$$

which is a constant, where μ is the permeability of the medium, and the radiation function R is given by

$$R = 2\pi\eta \sin\theta I(u)F(\mathbf{k}), \quad (2.4)$$

where θ is the angle between the direction of travel of the charged particle beam and the direction of propagation of the emitted radiation, $I(u)$ is the diffraction function, and $F(\mathbf{k})$ is the form factor. [Ref. 5: pp.2741,2742]

The wave vector of the emitted radiation is $\mathbf{k}$ ($k = \omega/c$), and $F(\mathbf{k})$ is the dimensionless form factor. That is, if $\rho(\mathbf{r})$ is the charge distribution of a single bunch, then the Fourier components of the charge are

$$\rho(\mathbf{k}) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \rho(\mathbf{r}) e^{i\mathbf{k} \cdot \mathbf{r}} d^3r, \quad (2.5)$$

and the form factor is defined by

$$\rho(\mathbf{k}) = qF(\mathbf{k}). \quad (2.6)$$

For a point charge, $F(\mathbf{k})$ is identically one for all values of $\mathbf{k}$.

The dimensionless beam length parameter η which is defined as the ratio of the path length of the charged particle beam to the wavelength in the medium of the emitted radiation, appears in the radiation function explicitly, and implicitly as part of the diffraction parameter defined below:

$$\eta = L / \lambda. \quad (2.7)$$

The diffraction function is

$$I(u) = \sin u/u, \quad (2.8)$$

where the dimensionless diffraction parameter u depends upon the Cerenkov angle given by $\cos \theta_c = (n\beta)^{-1}$, as well as upon the beam length parameter and the radiation emission angle:

$$u = \pi \eta [(n\beta)^{-1} - \cos \theta]. \quad (2.9)$$

The parameter η determines the periodicity of the diffraction pattern and also determines its magnitude. Since R depends directly upon η , the strength of the radiation is proportional to the square of the path length of the beam. [Ref. 5: pp. 2741,2742]

D. FINITE-LENGTH PATH

If the emission region has finite length, which may be realized by passing the electron beam through a gas cell, the radiation propagation direction is not confined to a sharp Cerenkov angle θ_c , but is spread over a range of emission angles. For the case of gas, for which the ordinary Cerenkov angle is a few degrees, the broadening is asymmetric about the Cerenkov cone, and the radiated power displays various interference lobes. This spreading effect depends only on the path length in the gas and does not depend on the electron bunch structure or periodicity of the bunches. [Ref. 3: pp. 3246,3251]

Radiation from the polarized molecules along the path of the electron beam is formally equivalent to diffraction from a single slit at angles far from normal incidence. The shift in the radiation peak can be understood as a

diffraction effect arising from the linearly varying phase of the radiation along the beam interaction length [Ref. 3: p. 3246].

Considerable power (about half in the case of a gas) appears outside the main lobe, and the latter is peaked at angles much larger than the Cerenkov angle. The Cerenkov power radiated per unit path length is increased by large factors approaching 2 orders of magnitude for a gas path of finite length compared to one of infinite length [Ref. 3: p. 3251].

This increase in power is associated with the finite length of the radiating medium only. The effect should be approximately the same for either single or periodic electron bunches and should occur whether the bunches are effectively point charges or have significant size.

The value of the parameter u is affected by η and the beam energy through β . As either of these parameters is varied, the angular position of the zeros of $I(u)$ changes. The emission threshold is defined as the situation when the first zero of the diffraction function enters the physical range. Applying this criterion, the result is that for small values of η , a Cerenkov-like radiation pattern is produced even when the product $n\beta < 1$. That is, the threshold occurs for $n\beta < 1$ at small values of η . As η increases (at constant $n\beta < 1$), the threshold is crossed and the radiation pattern becomes more chaotic. A full discussion of these geometrical effects is given in Ref. 5.

E. PERIODIC ELECTRON BUNCHES

Cerenkov radiation was considered for periodic bunches of electrons such as would be emitted by a typical traveling-wave electron linear accelerator (LINAC). Because the distribution of intensity of Cerenkov is proportional to the frequency, the radiation at microwave frequencies would be low unless

beams are intense and bunched so that coherent radiation by many electrons contributes [Ref. 2: p. 1531].

Periodic bunches of electrons produce Cerenkov radiation at harmonics of the bunch frequency, while a single bunch will radiate with a continuous frequency distribution. The effect of bunch size is reflected in the factor of the Fourier transform of the charge in the bunch, which causes the radiation to fall off at high frequencies, while at low frequencies all charges in the bunch radiate in phase.

At low frequencies such that the wavelength of the emitted radiation is of the order of the bunch size, the electrons in the bunch radiate coherently. This leads to large enhancement factors for typical bunches consisting of 10^8 electrons, and in fact allows the radiation to be significant at microwave frequencies. [Ref. 3: p. 3246]

At higher frequencies or harmonics, destructive interference, described by the Fourier transform of the charge density, decreases intensities with increasing frequency, until incoherent radiation takes over when the wavelength of the radiation is much less than electron spacing [Ref. 3: p. 3246].

When a single electron passes through a dielectric medium where a spatially periodic term is added to the dielectric constant, the result is radiation occurring even for electrons which do not exceed the velocity of light in the medium and at angles other than the Cerenkov cone angle. The non-Cerenkov part of the radiation is attributed to transition radiation. If the electron velocity were lower so that v/c were close to but less than unity, the peak in I would be pushed to the left toward 0° of θ such that $\cos \theta_c = v/c$ would be larger than 1. But the tails of the diffraction function I could extend

into the physical range $1 \geq \cos \theta \geq -1$, and this would be called transition radiation and be ascribed to the passage of the electrons through the boundaries of the gas cell. [Ref. 2: p. 1535]

F. PROFILE DETERMINATION OF A ELECTRON BEAM BUNCH

1. Effect of The Form Factor

The bunch form factors are Fourier Transforms $F(\mathbf{k})$ which differ depending on the charge distribution within a bunch. The form factor is identically one for a point charge, and for a finite charge distribution $F(\mathbf{k}) = 1$ for $\mathbf{k} = 0$. If all the charge within a bunch is of the same sign $F(\mathbf{k})$ must fall off as a function of k near the origin. Here we consider only line charge distribution and consequently the form factors are functions of the product of $k_z = k \cos \theta$ and appropriate lengths which are characteristic of the charge distribution of a bunch.

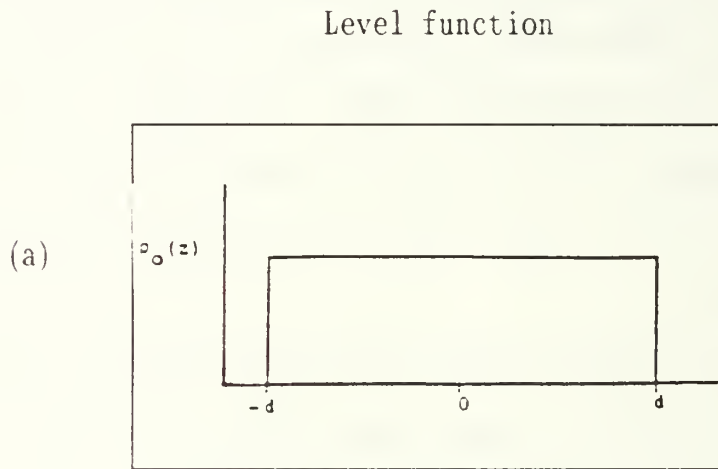
Thus the behavior of the form factor F over the range of emission angles is dependant on the ratio of the charge bunch lengths to the wavelength of the emitted radiation. For a small value of these ratios, the value of F is essentially unity for all angles. Then the emitted radiation pattern is modulated only by the geometrical envelope function as described in Ref. 5.

However for larger values of the ratios, the value of F over the range of emission angles can be significantly less than one. In this case the dependence of the form factor on angle is dramatic since the cosine term goes to zero at ninety degrees causing a form factor of unity. If, at same time the emission length ratio is small, a condition could be achieved where the majority of the Cerenkov power is radiated in a direction normal to the electron beam path.

A complete angular map of Cerenkov radiation patterns may be used to characterize the properties of relativistic beam pulses, and may enable one to determine the beam pulse charge distribution from measured radiated patterns [Ref. 4: p. 1996].

2 Bunch Shapes and Corresponding Form Factors

Figure 2.3 diagrams the beam pulse shapes and presents the corresponding form factor expressions. [Ref. 8: pp. 16,17]

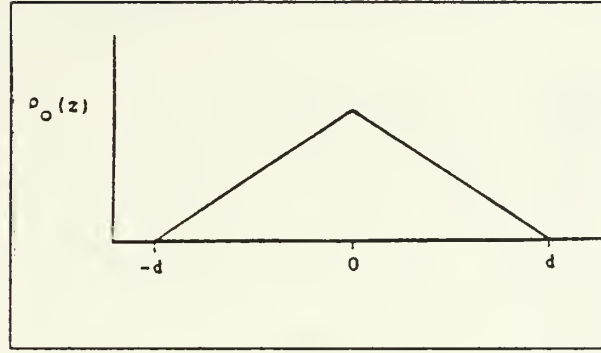


$$F(k_z) = \frac{\sin k_z d}{k_z d}$$

Figure 2.3 Electron Beam Charge Bunch Shapes and Corresponding Form Factors.

Triangular function.

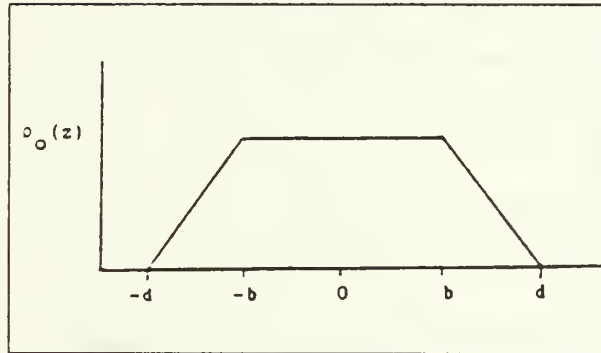
(b)



$$F(k_z) = Ad \left[\frac{\sin \frac{k_z d}{2}}{\frac{k_z d}{2}} \right]^2$$

Trapezoidal function

(c)



$$F(k_z) = AL \left[\frac{\sin \frac{k_z \ell}{2}}{\frac{k_z \ell}{2}} \times \frac{\sin \frac{k_z l}{2}}{\frac{k_z l}{2}} \right]$$

where $\ell = (l_t + l_b)/2$, $l = (l_b - l_t)/2$,

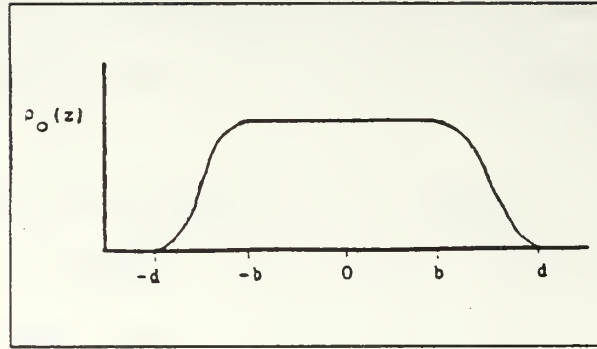
l_t = top level length of trapezoidal.

l_b = bottom level length of trapezoidal.

Figure 2.3 (cont.) Electron Beam Charge Bunch Shapes and Corresponding Form Factors.

Rounded function

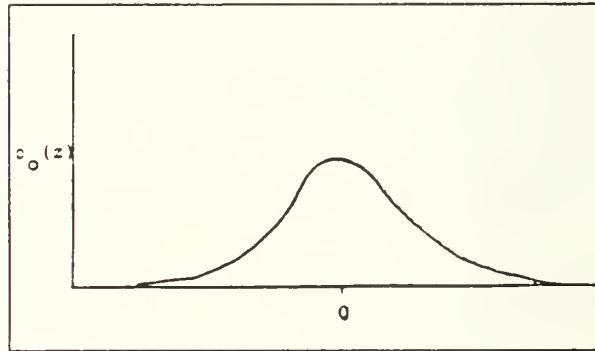
(d)



$$F(k_z) = \frac{8}{k_z^3(b+d)(d-b)^2} \left[2 \sin \frac{k_z}{2} (d+b) - \sin k_z b - \sin k_z d \right]$$

Gaussian function

(e)

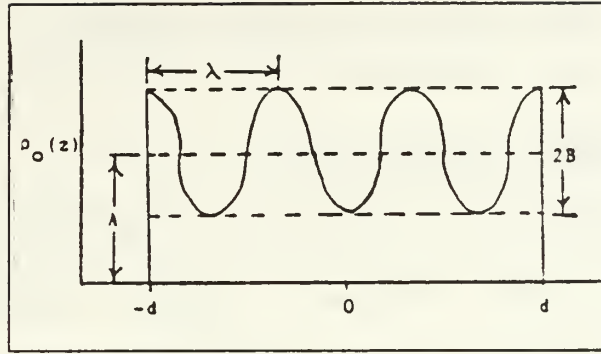


$$F(k_z) = e^{-\left[\frac{k_z b}{2}\right]^2} \quad \text{where } b = \text{bunch size.}$$

Figure 2.3 (cont.) Electron Beam Charge Bunch Shapes and Corresponding Form Factors.

Level Plus Ripple function

(f)

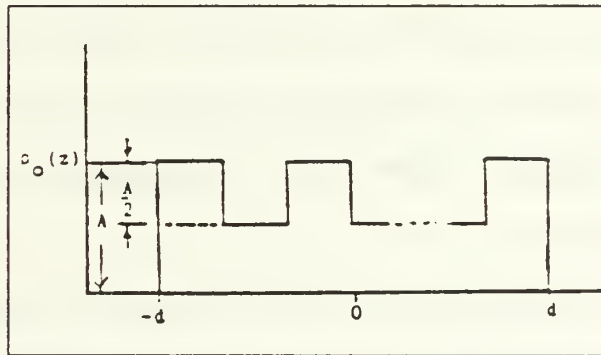


$$F(k_z) = \frac{\sin k_z d}{k_z d} + \frac{R}{2} \left[\frac{\sin(k_z + k_0)d}{(k_z - k_0)d} + \frac{\sin(k_z - k_0)d}{(k_z + k_0)d} \right]$$

where $R = B/A$ $k_0 = 2\pi/\lambda$

Multiple Hump function

(g)



$$F(k_z) = \frac{2\sin k_z d}{k_z d} - \frac{\sin k_z d \left[\frac{2N-3}{2N-1} \right]}{k_z} \Big|_{N=2} + \frac{\sin k_z d \left[\frac{2N-5}{2N-1} \right]}{k_z d} \Big|_{N=3}$$

where $N = \text{number of humps.}$

Figure 2.3 (cont.) Electron Beam Charge Bunch Shapes and Corresponding Form Factors.

III. CALCULATION AND RESULTS

A. PARAMETERS FOR CALCULATION

Professor J. R. Neighbours and others of the Department of Physics, Naval Postgraduate School, Monterey, California, developed a computer program to calculate and plot angular maps of the radiated energy per unit solid angle for a given form factor. The program originally was designed to run on a Tektronix Computer and considered the following one dimensional (i.e. in Z only) beam charge distributions: Gaussian, level (i.e. boxcar), level plus a sinusoidal, ripple combination, and a double hump.

This work was aimed to modify the program to run on the IBM 370 mainframe computer and plot the calculated power per solid angle, radiated at the frequency ν , using the DISSPLA V10.5. The results are limited to the three form factors for the rectangular, Gaussian and trapezoidal charge distributions. Calculations for other charge distributions are left for future work.

To calculate the total coherent power per unit solid angle, radiated at the frequency ν by a periodic charged particle beam in traveling a finite distance L at constant velocity, a set of parameters were chosen close to those available in an experiment.

- (1) Index of refraction, $n = 1.000268$.
- (2) Speed of light in vacuum, $c_0 = 2.997925 \times 10^8$ m.
- (3) Fundamental frequency, $\nu_0 = 2.85$ GHz.
- (4) Bunch charge, $B = 1.5 \times 10^{-12}$ Coulomb.

These values give an $n\beta$ product of $n\beta = 0.98$, which is 2 % below the infinite path length threshold value of unity. By choosing different radiation harmonics and varying the path length the radiation pattern above ($\eta = 12$) and below ($\eta = 37$) the threshold for 2.555 Mev electron bunches, could be investigated. The calculations were carried out at constant η for the various charge distribution as the size of the distribution was varied.

B. GAUSSIAN FUNCTION

Fig. 3.1 through Fig. 3.8 show the radiation intensity pattern of Gaussian line charge distributions in sub-Cerenkov radiation ($n\beta = 0.98$) for two different value of η . Fig. 3.1 through Fig. 3.4 are the results of using $\eta = 12$, with $N = 3$, varying the bunch length from 0.24 cm to 2.4 cm. The rest of them are for the case of using $\eta = 37$, and likewise, varying the bunch length. BL is the symbol used for bunchlength.

Figures 3.1–3.4 show the effect on the emitted radiation pattern as the bunch length is increased while the beam path parameter η is held constant at $\eta = 12$. With a bunch length of 0.24 cm the radiation pattern is essentially that of a periodic set of point charges. As the bunch length increases, a hump first becomes evident in Fig. 3.2 when the wavelength of the emitted radiation begins to become comparable to the size of the bunch. Further increase in bunch size shows an increasing dominance of the form factor until finally the radiation pattern is almost completely dependant on the form factor. In Fig. 3.4 the envelope of the radiation pattern is the form factor for the Gaussian charge distribution except for a slight skewing caused by the geometrical envelope function.

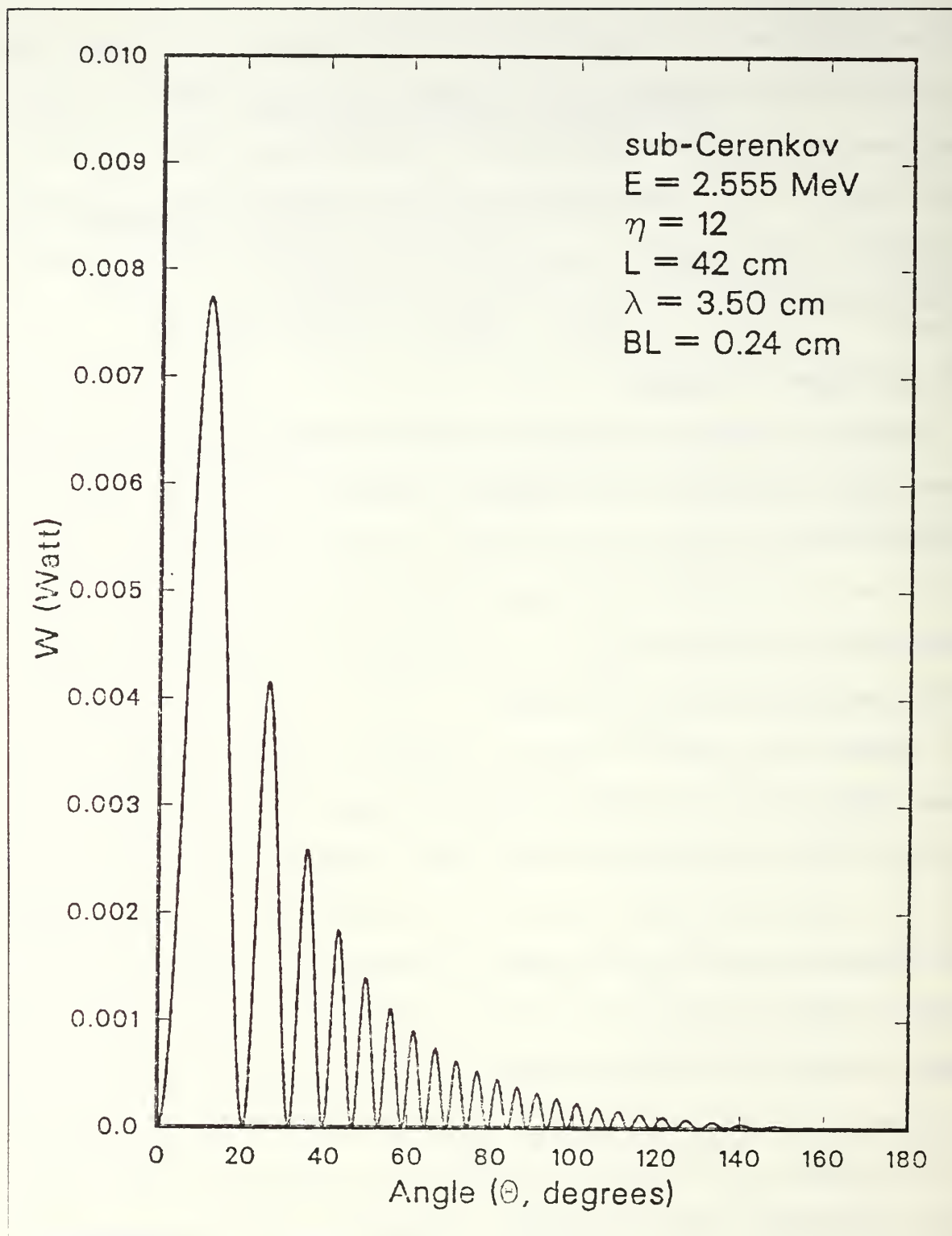


Fig. 3.1 Gaussian Function with $BL/\lambda = 0.069$, $\eta = 12$

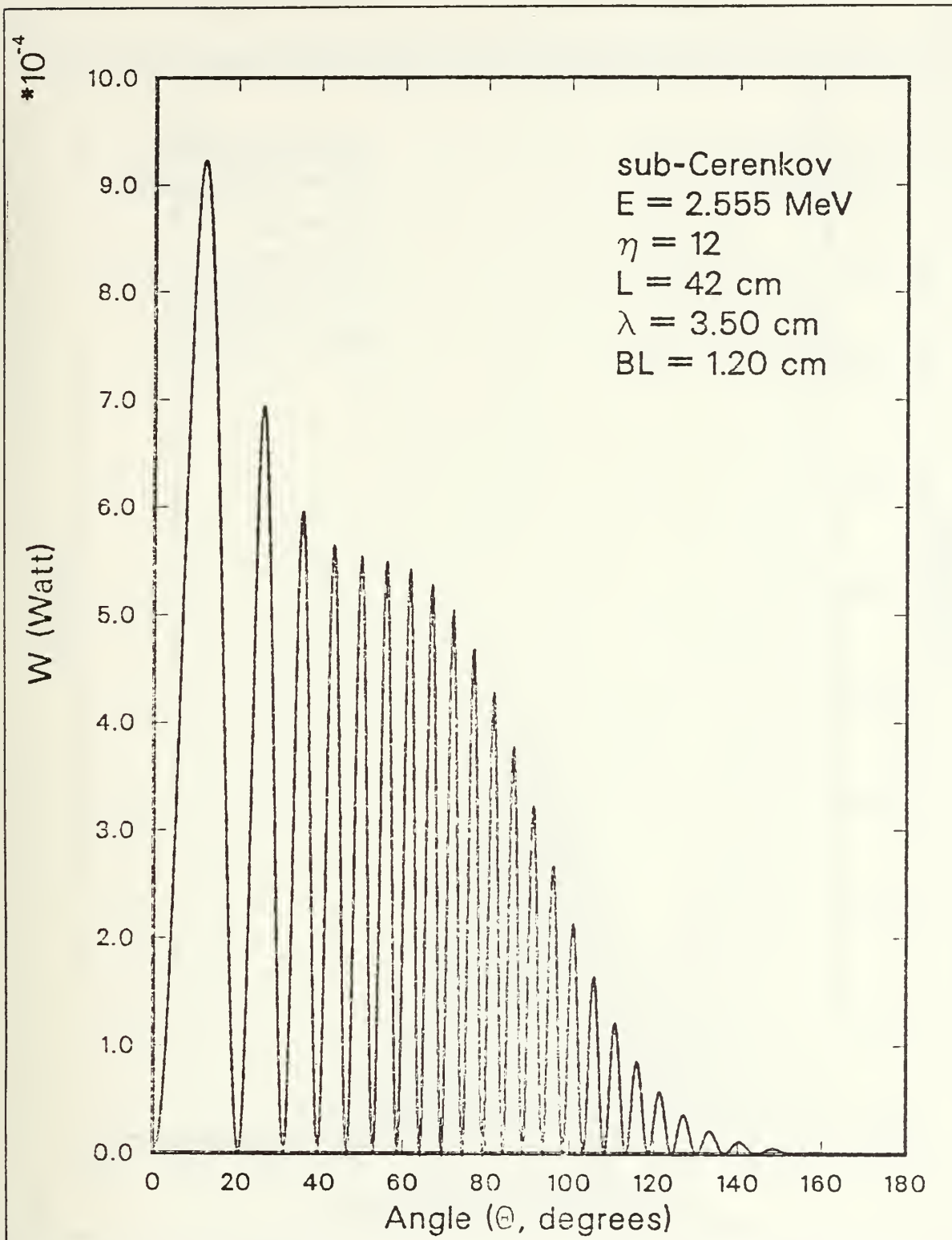


Fig. 3.2 Gaussian Function with $BL/\lambda = 0.343$, $\eta = 12$

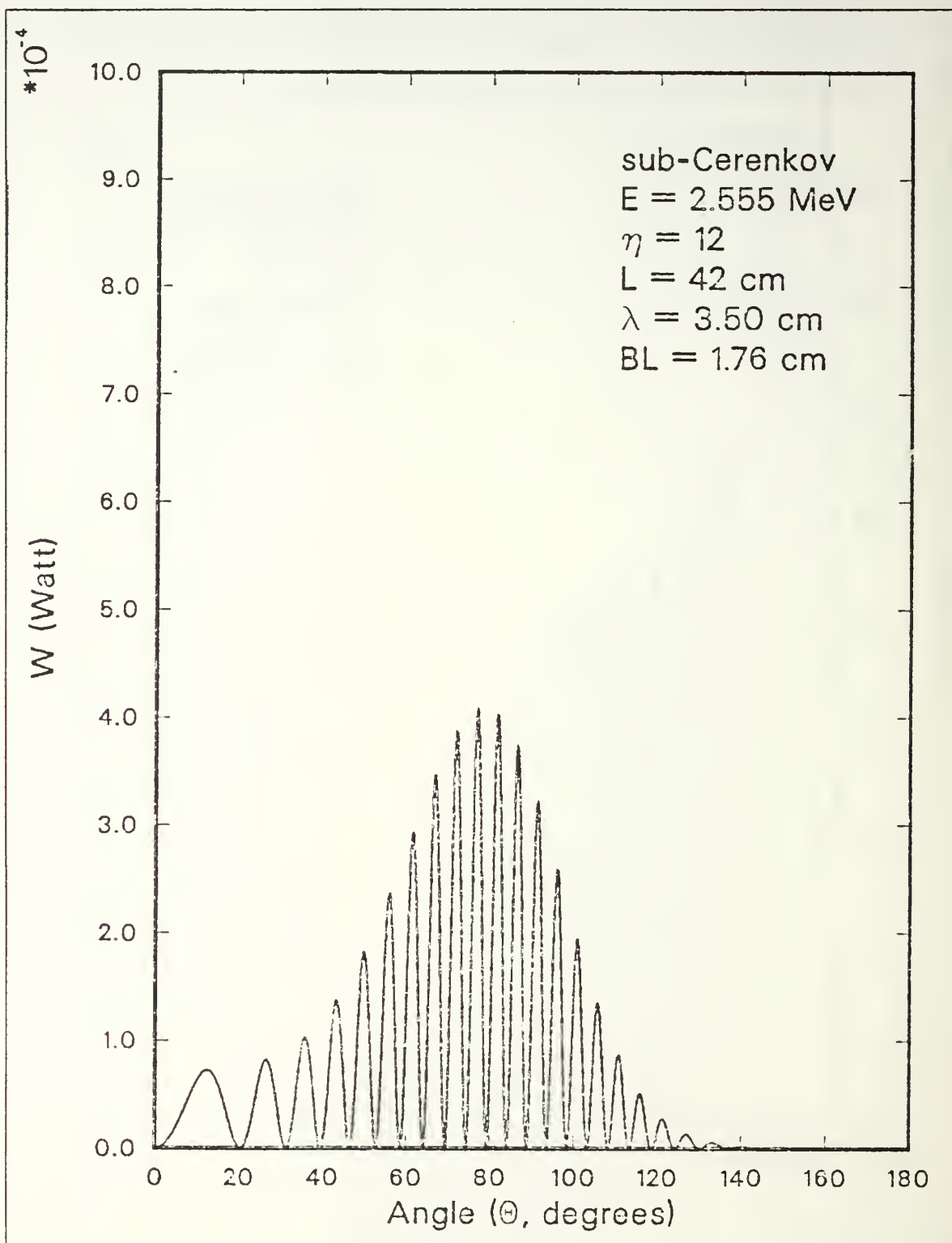


Fig. 3.3 Gaussian Function with $BL/\lambda = 0.503$, $\eta = 12$

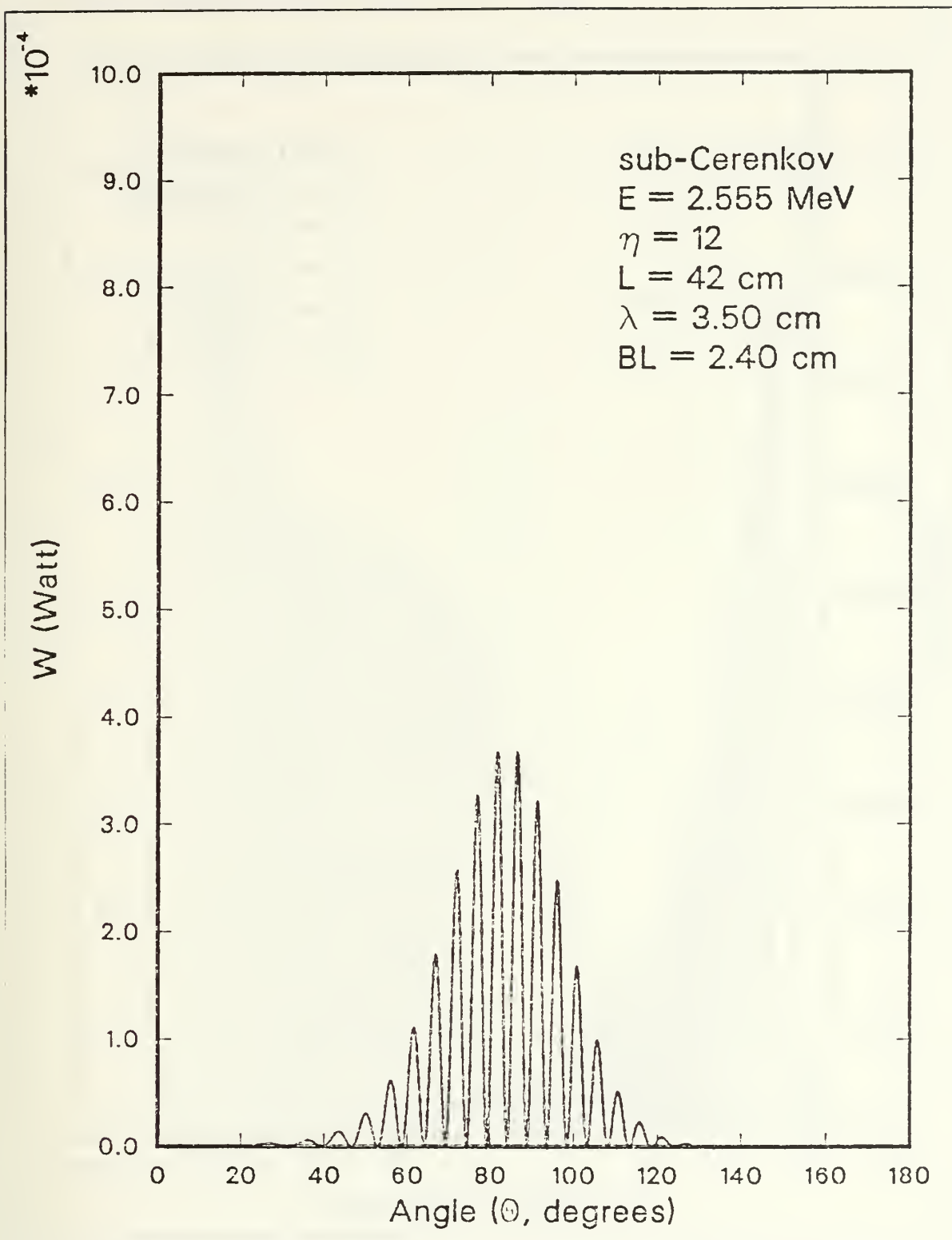


Fig. 3.4 Gaussian Function with $BL/\lambda = 0.686$, $\eta = 12$

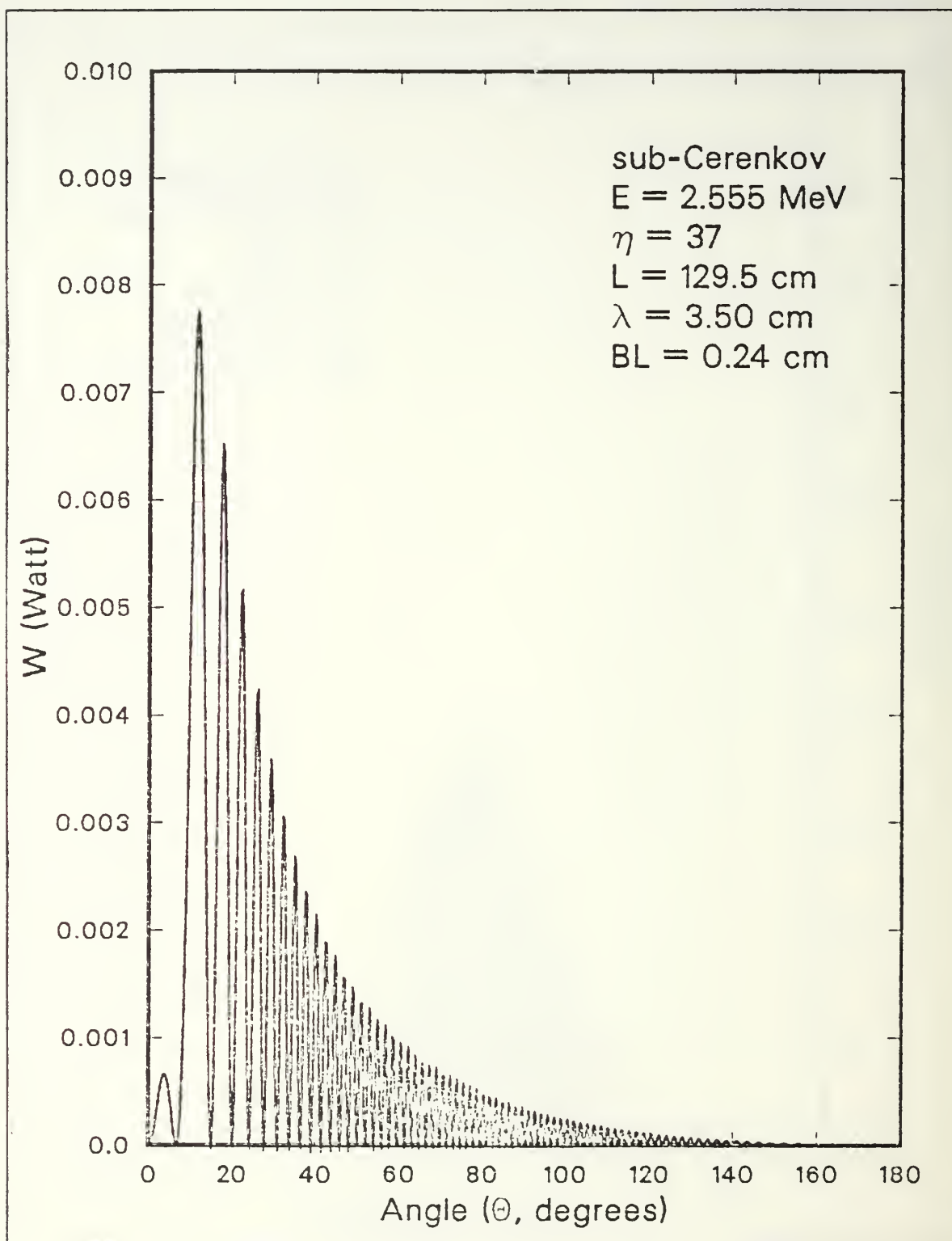


Fig. 3.5 Gaussian Function with $BL/\lambda = 0.069$, $\eta = 37$

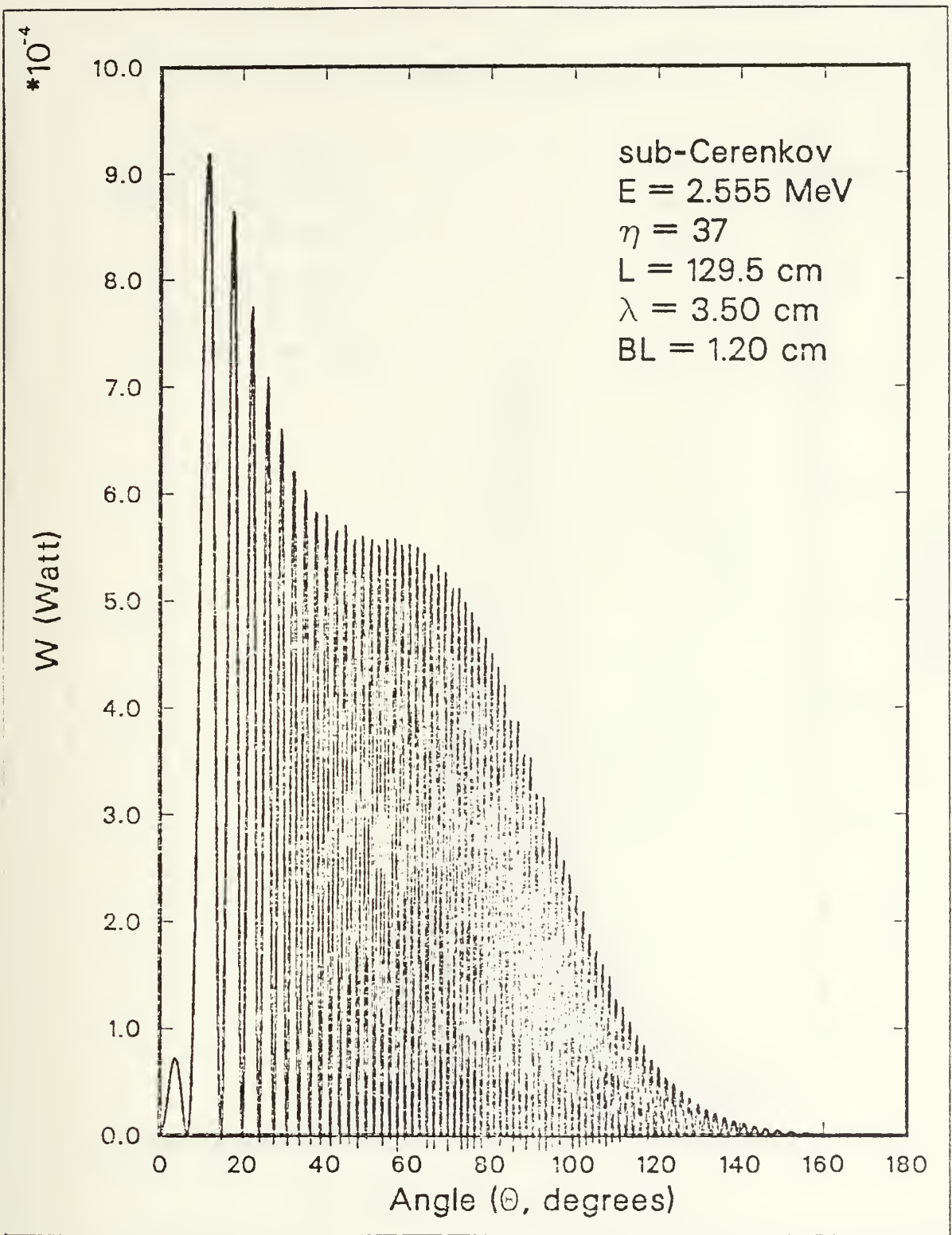


Fig. 3.6 Gaussian Function with $BL/\lambda = 0.343$, $\eta = 37$

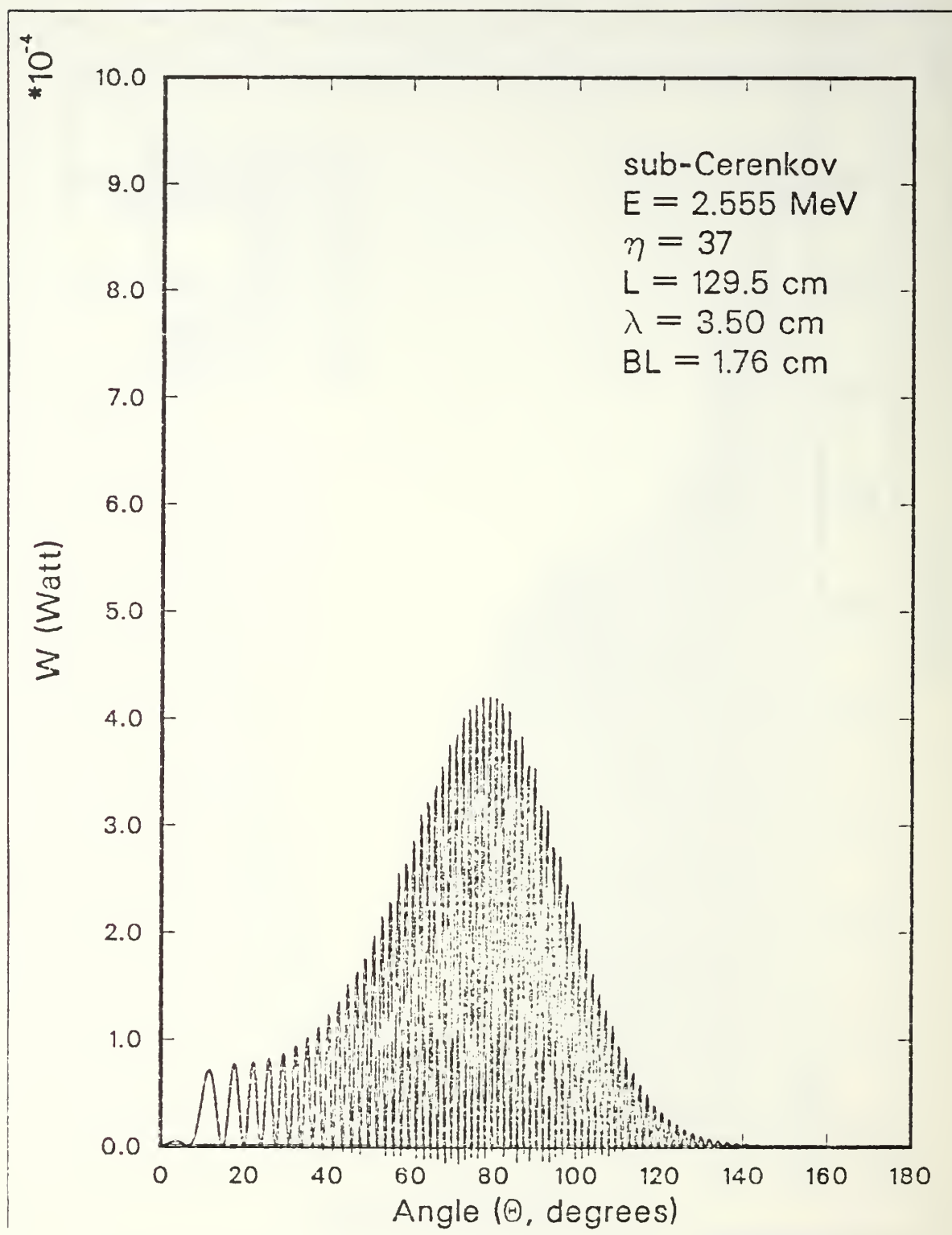


Fig. 3.7 Gaussian Function with $BL/\lambda = 0.503$, $\eta = 37$

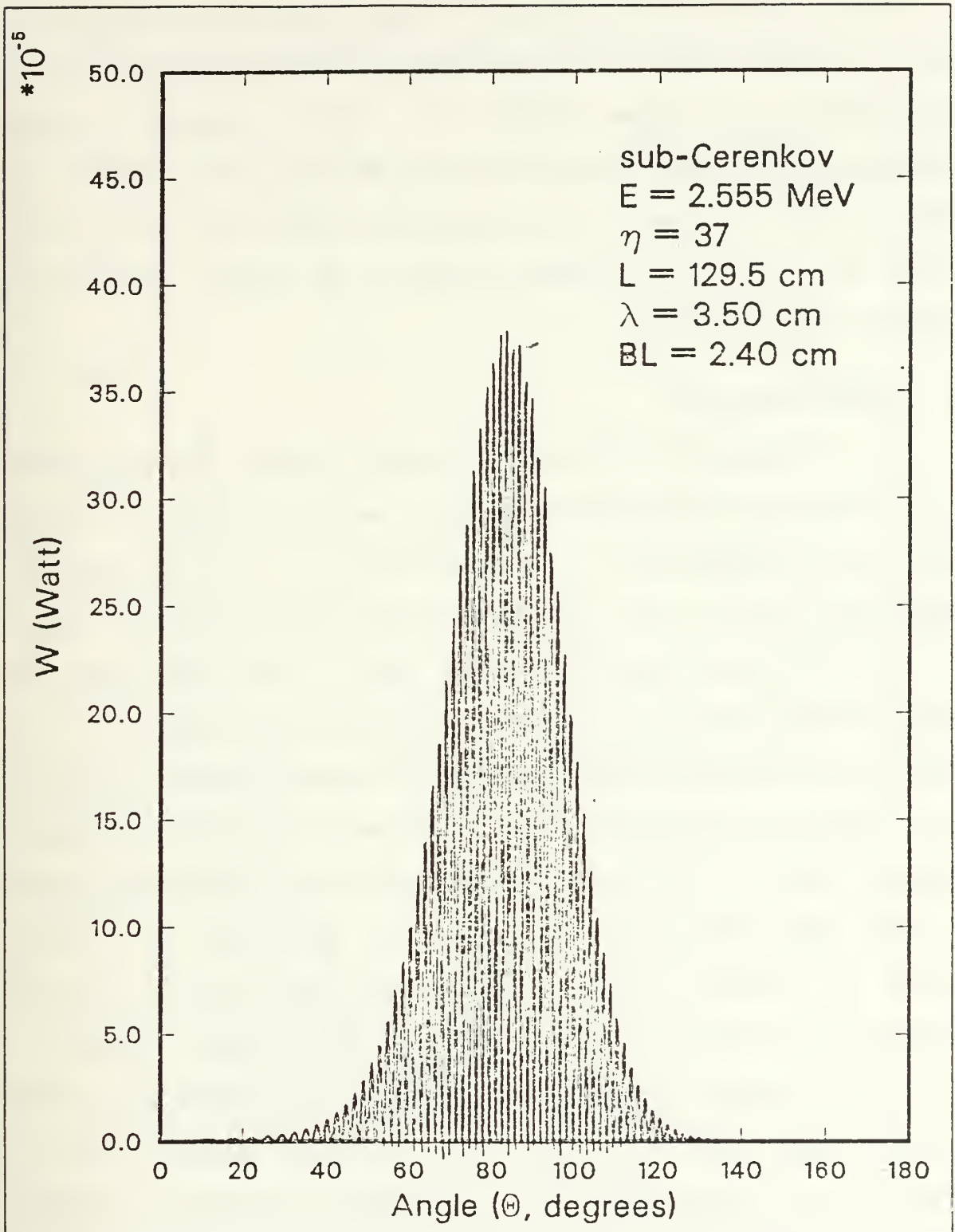


Fig. 3.8 Gaussian Function with $BL/\lambda = 0.686$, $\eta = 37$

Similar remarks can be made for the longer finite path results shown in Fig. 3.5 – 3.8 for $\eta = 37$. In this set of figures, because this value of η causes the radiation to be below threshold, the radiation patterns are wildly oscillating – almost chaotic. However exactly the same thing happens to the envelope of the radiation. Fig. 3.8, calculated for a bunch length of 2.4 cm, as is Fig. 3.4, also shows the radiation envelope to be the form factor for the Gaussian charge distribution.

C. LEVEL FUNCTION

Fig. 3.9 through Fig. 3.22 show the radiation intensity lobe development as the level function charge distribution length varies for the same two values of η . Fig. 3.9 through Fig. 3.15 are calculated for $\eta = 12$, the remainder through Fig. 3.22 for $\eta = 37$. LFL is the symbol for the level function length.

In Fig. 3.9, where the level function length is much smaller than the radiation length, the radiation pattern is almost the same shape as Fig. 3.1 which is for the Gaussian charge distribution. Proceeding through to Fig. 3.13, as the length of the charge distribution is increased the form factor becomes prominent. Fig. 3.13 is of interest in that it also shows considerable radiation at small angles. This result occurs because the form factor for the level function has secondary maximum which at low angles combine with the relatively large value of the diffraction function to give substantial radiation.

Further increases in level function length give an increased role to the form factor until finally in Fig. 3.15, it has become dominant. Here the envelope of the radiation is seen to be the (skewed) form factor of the level function. The small lone peak at approximately ten degrees occurs at the maximum of the geometrical envelope function.

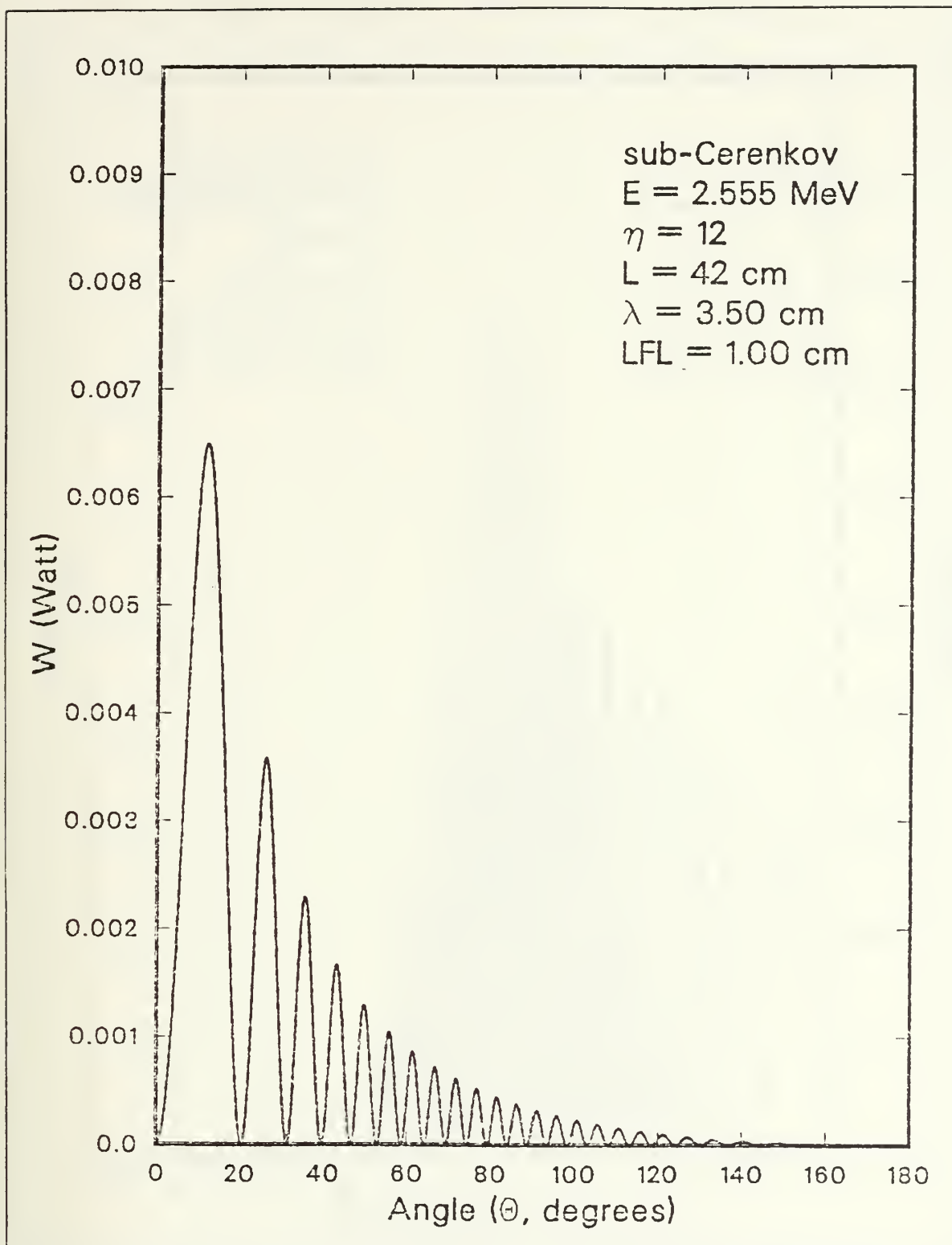


Fig. 3.9 Level Function with $LFL/\lambda = 0.285$, $\eta = 12$

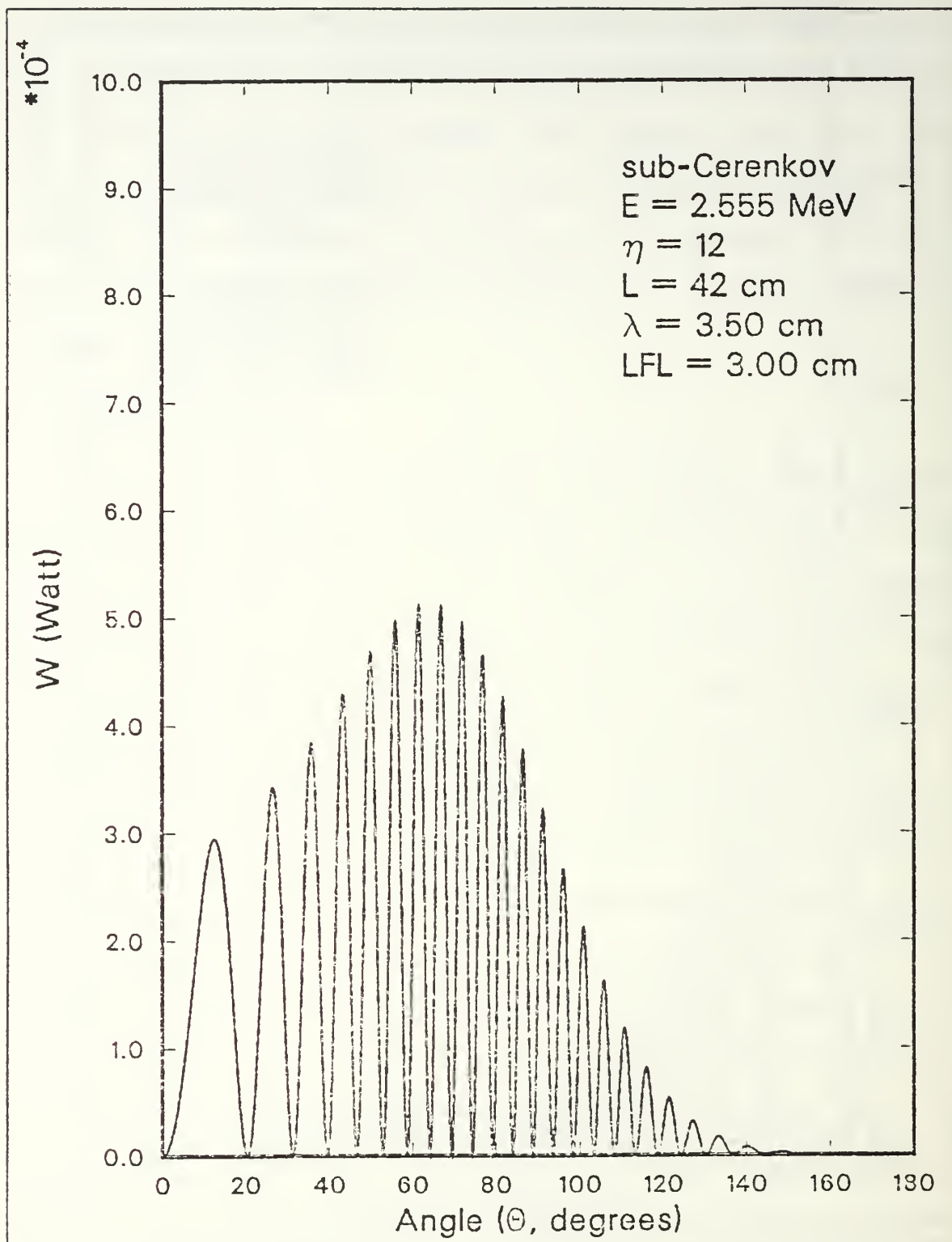


Fig. 3.10 Level Function with $LFL/\lambda = 0.855$, $\eta = 12$

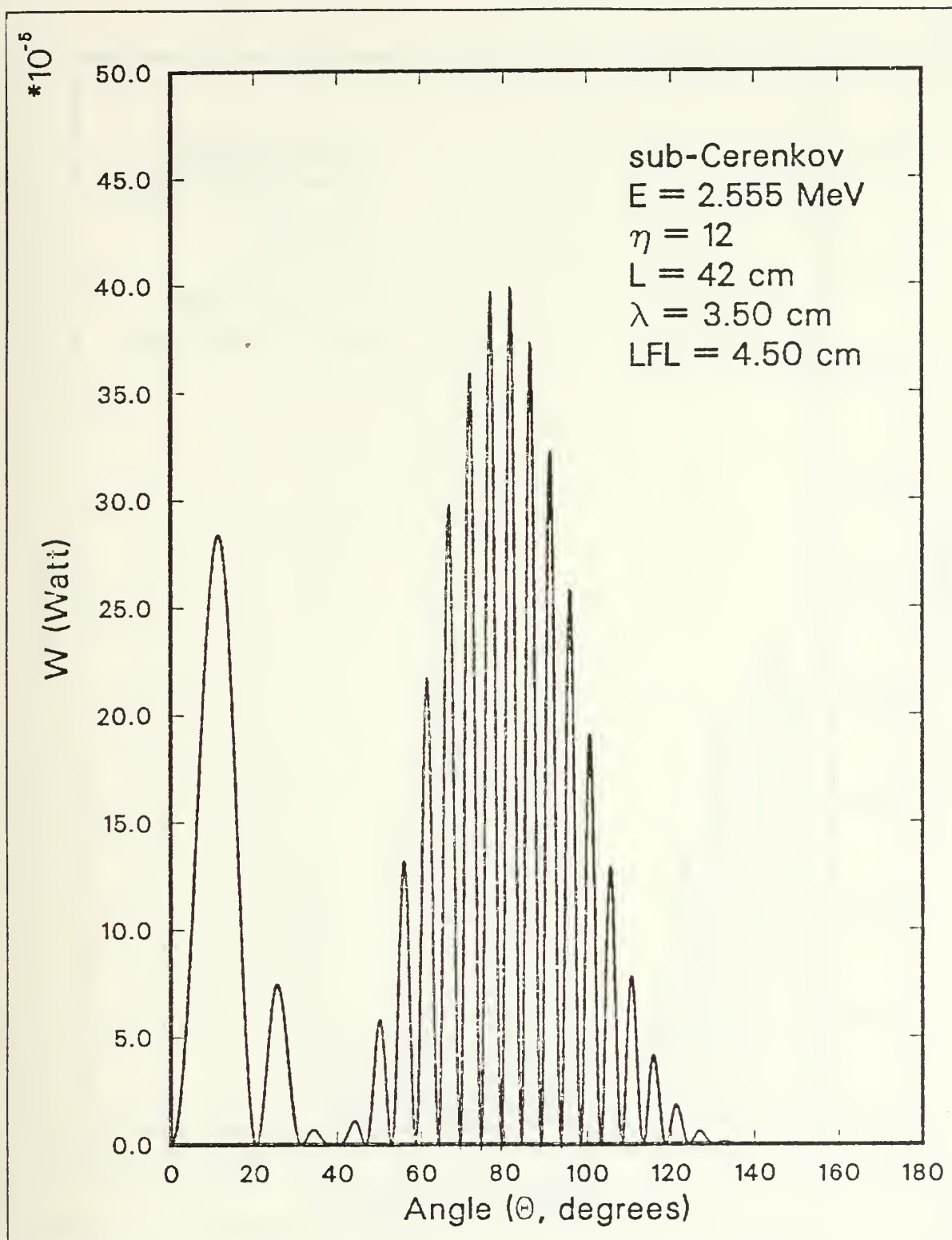


Fig. 3.11 Level Function with $LFL/\lambda = 1.28$, $\eta = 12$

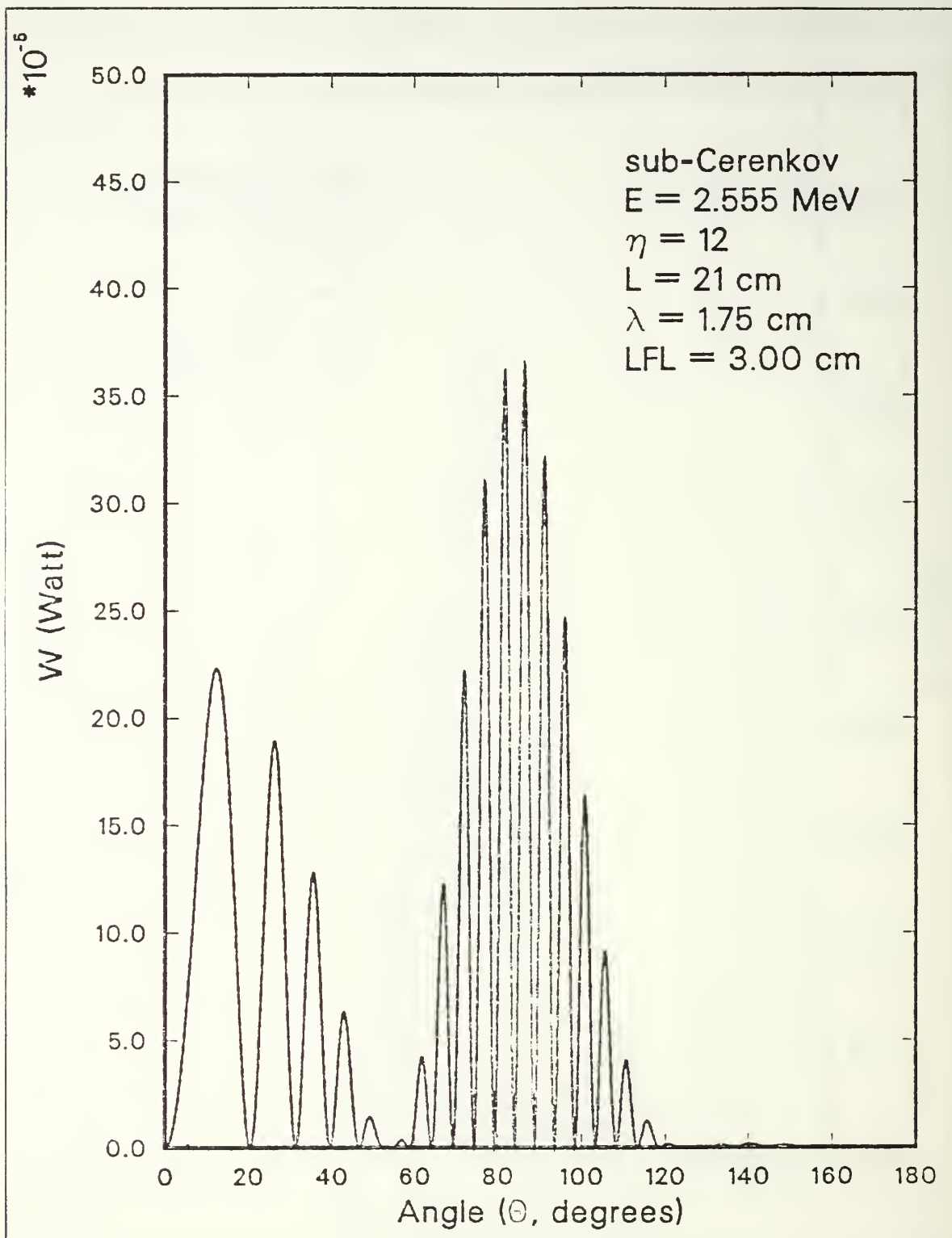


Fig. 3.12 Level Function with $LFL/\lambda = 1.71$, $\eta = 12$

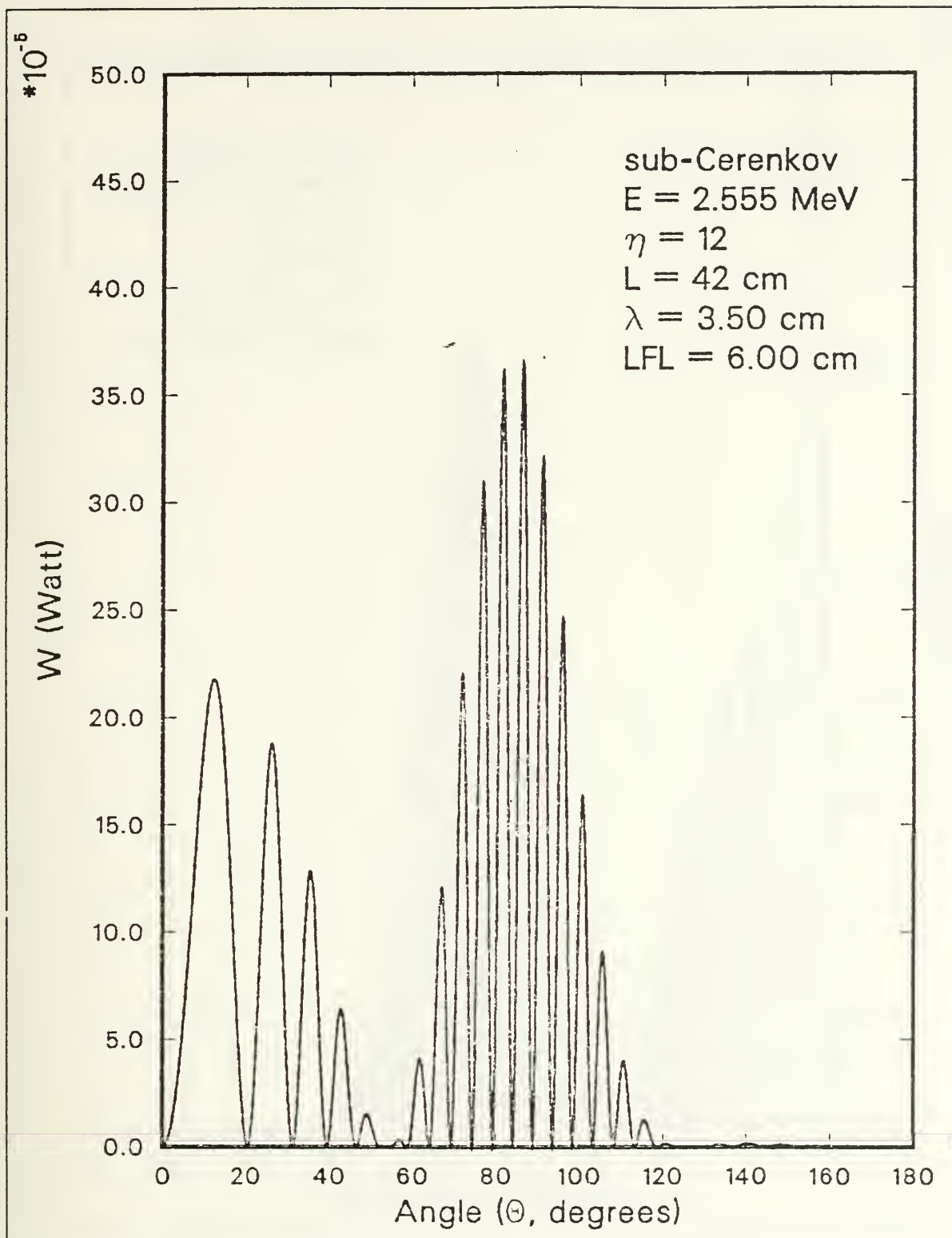


Fig. 3.13 Level Function with $LFL/\lambda = 1.71$, $\eta = 12$

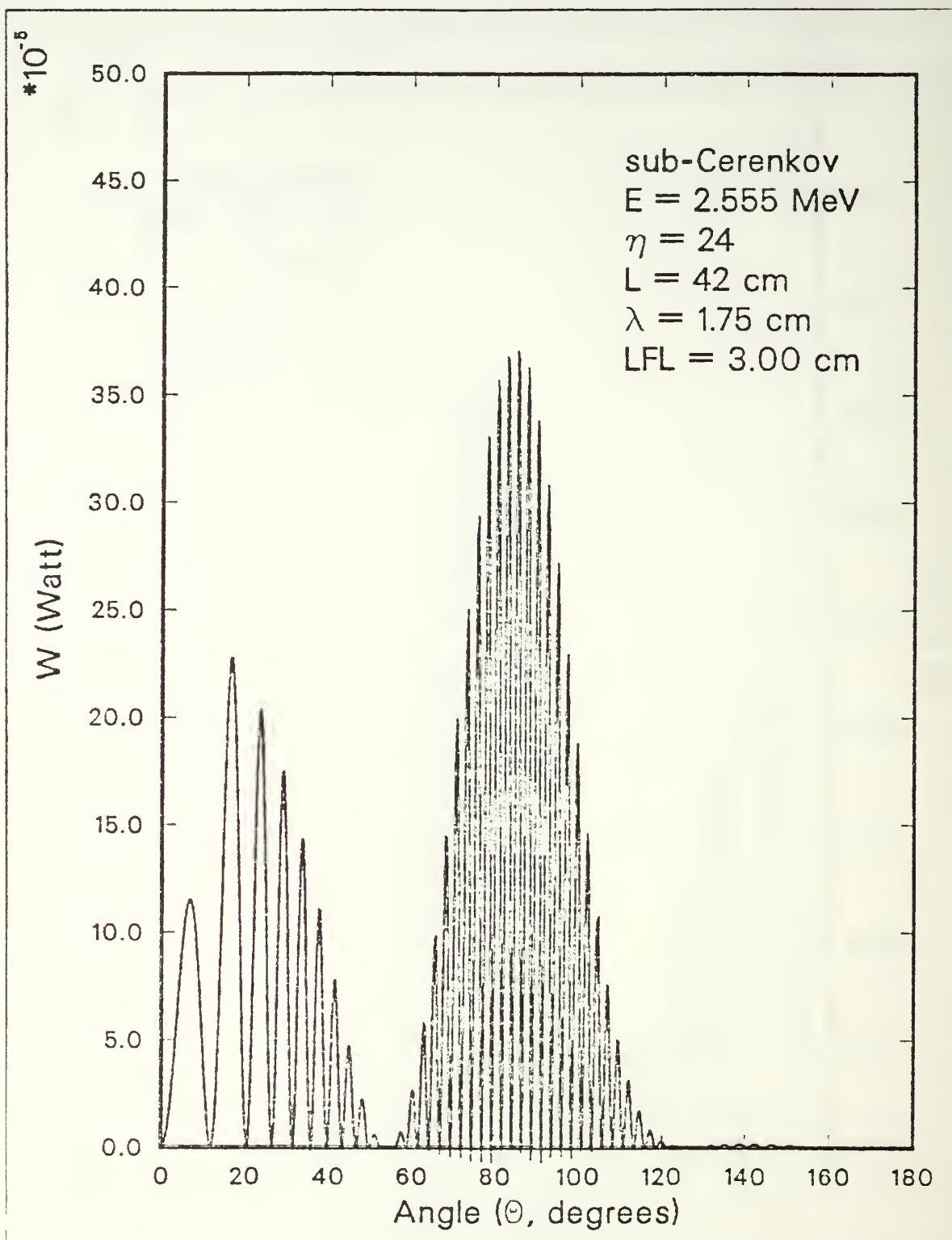


Fig. 3.14 Level Function with $LFL/\lambda = 1.71$, $\eta = 24$

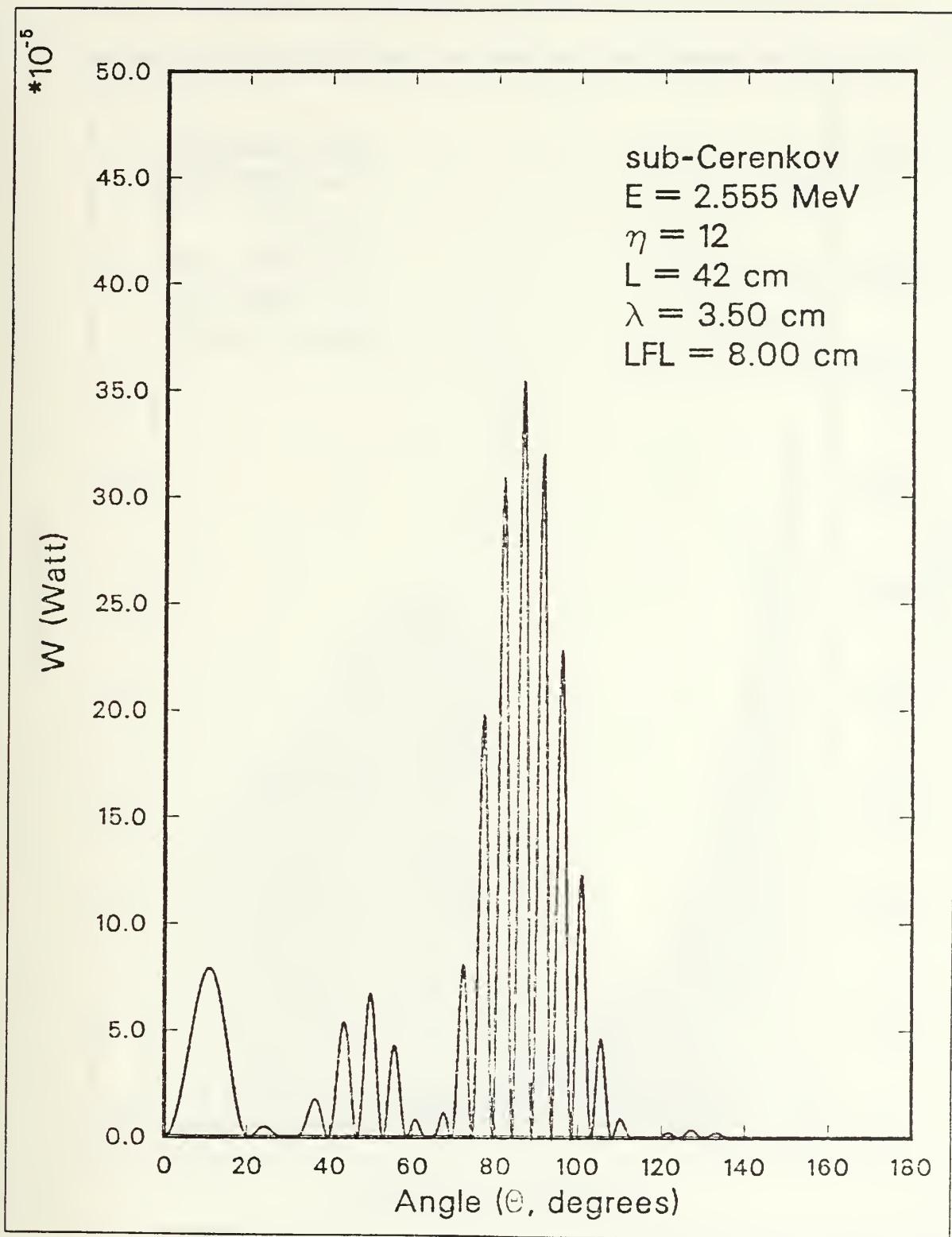


Fig. 3.15 Level Function with $LFL/\lambda = 2.28$, $\eta = 12$

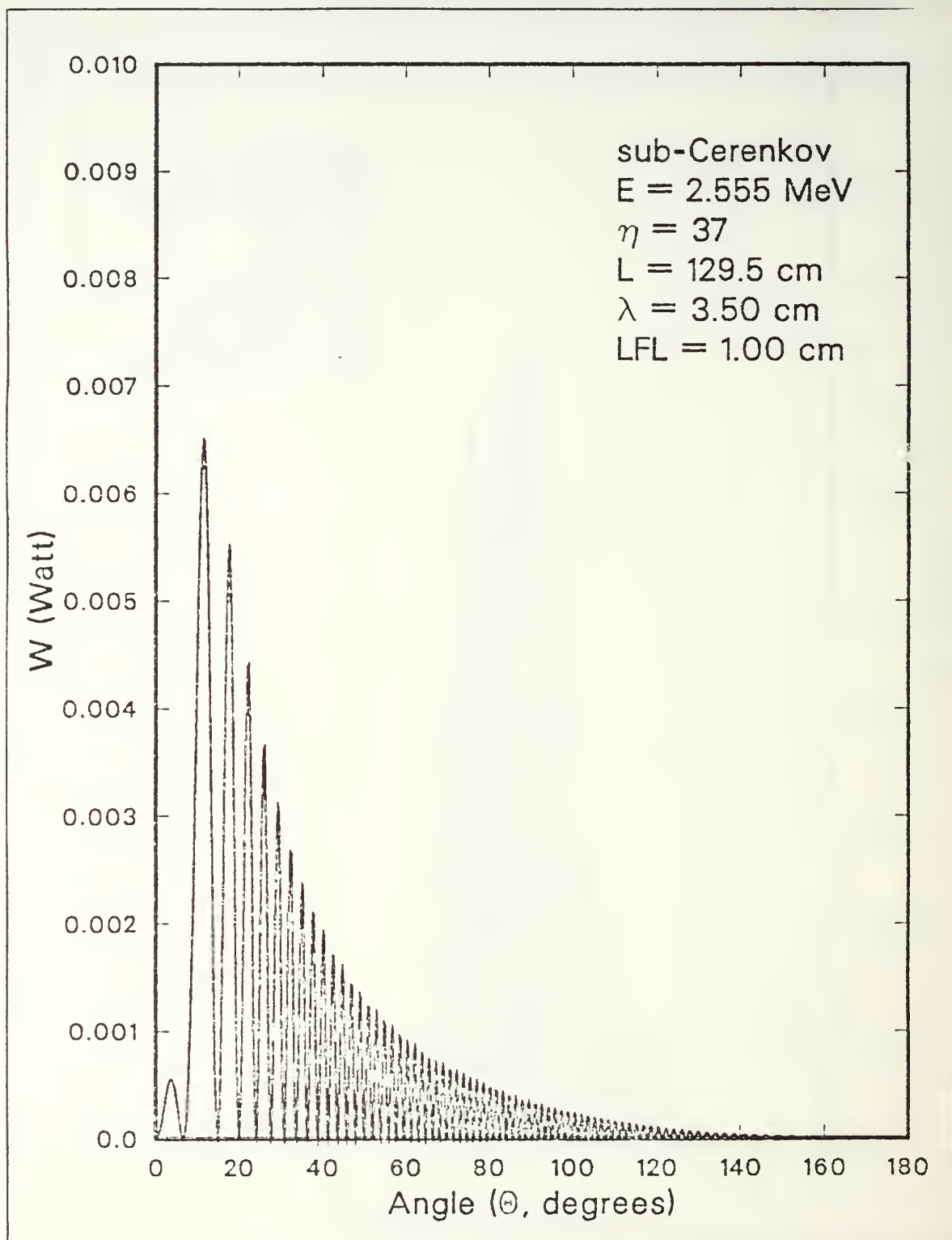


Fig. 3.16 Level Function with $LFL/\lambda = 0.29$, $\eta = 37$

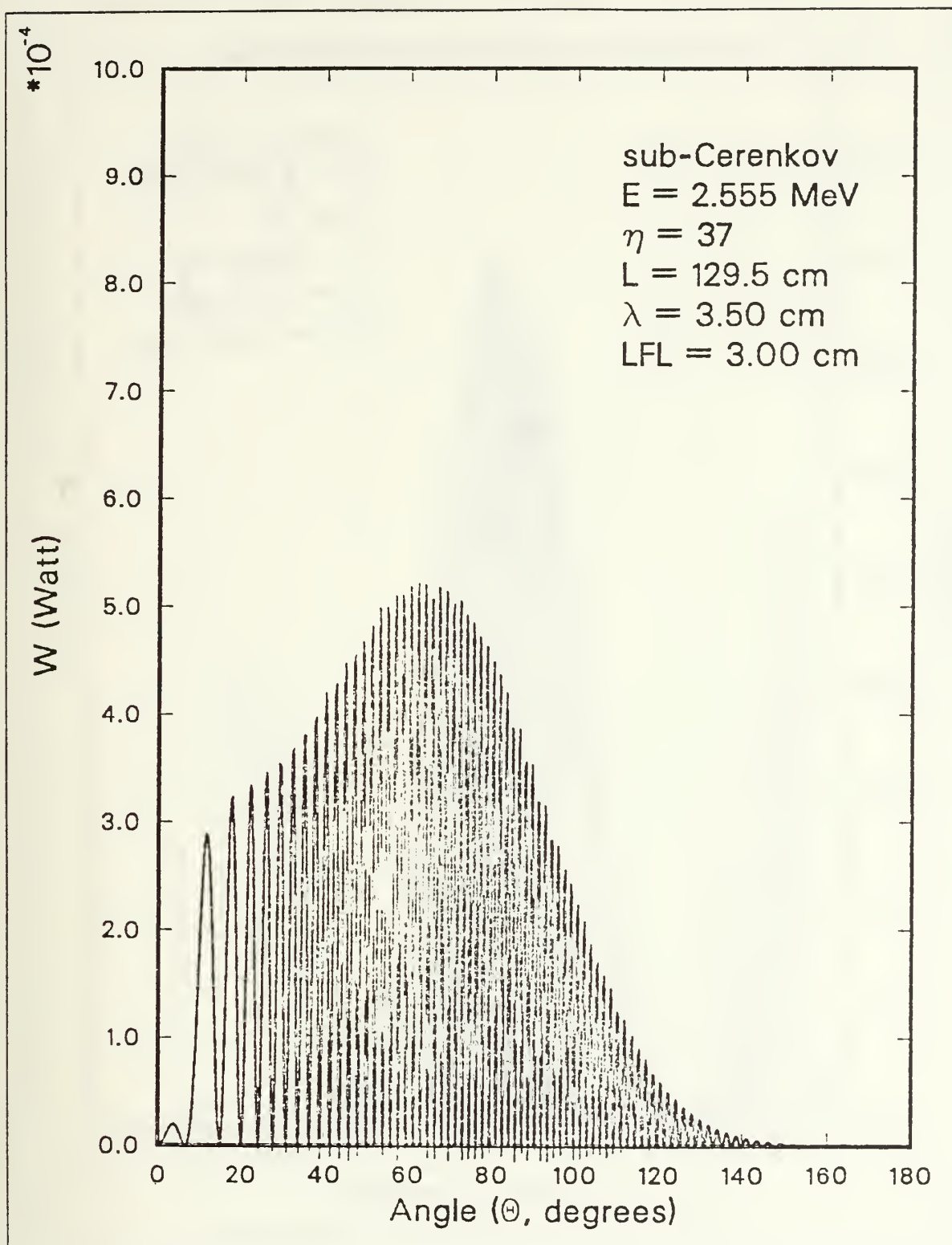


Fig. 3.17 Level Function with $LFL/\lambda = 0.85$, $\eta = 37$

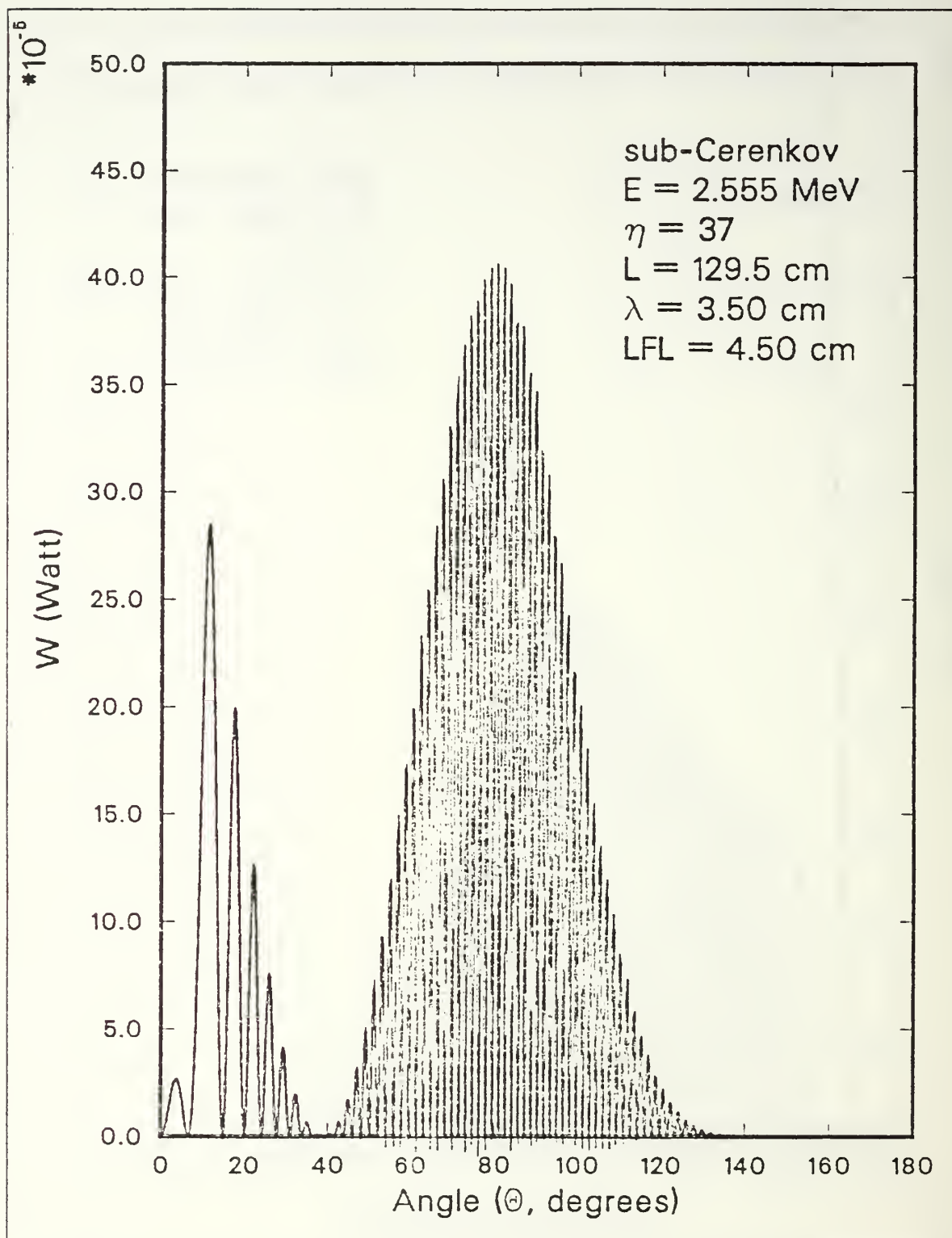


Fig. 3.18 Level Function with $LFL/\lambda = 1.28$, $\eta = 37$

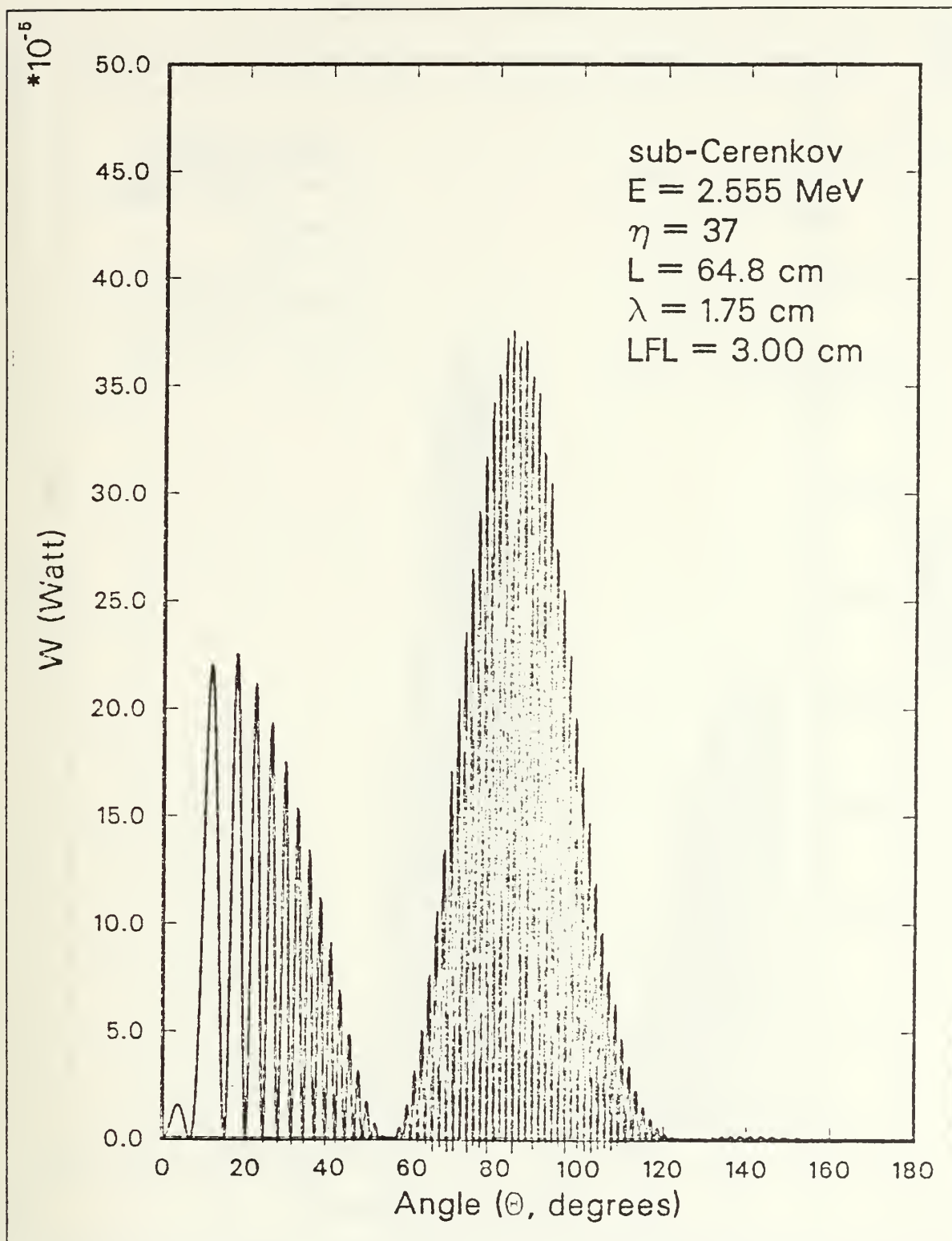


Fig. 3.19 Level Function with $LFL/\lambda = 1.71$, $\eta = 37$

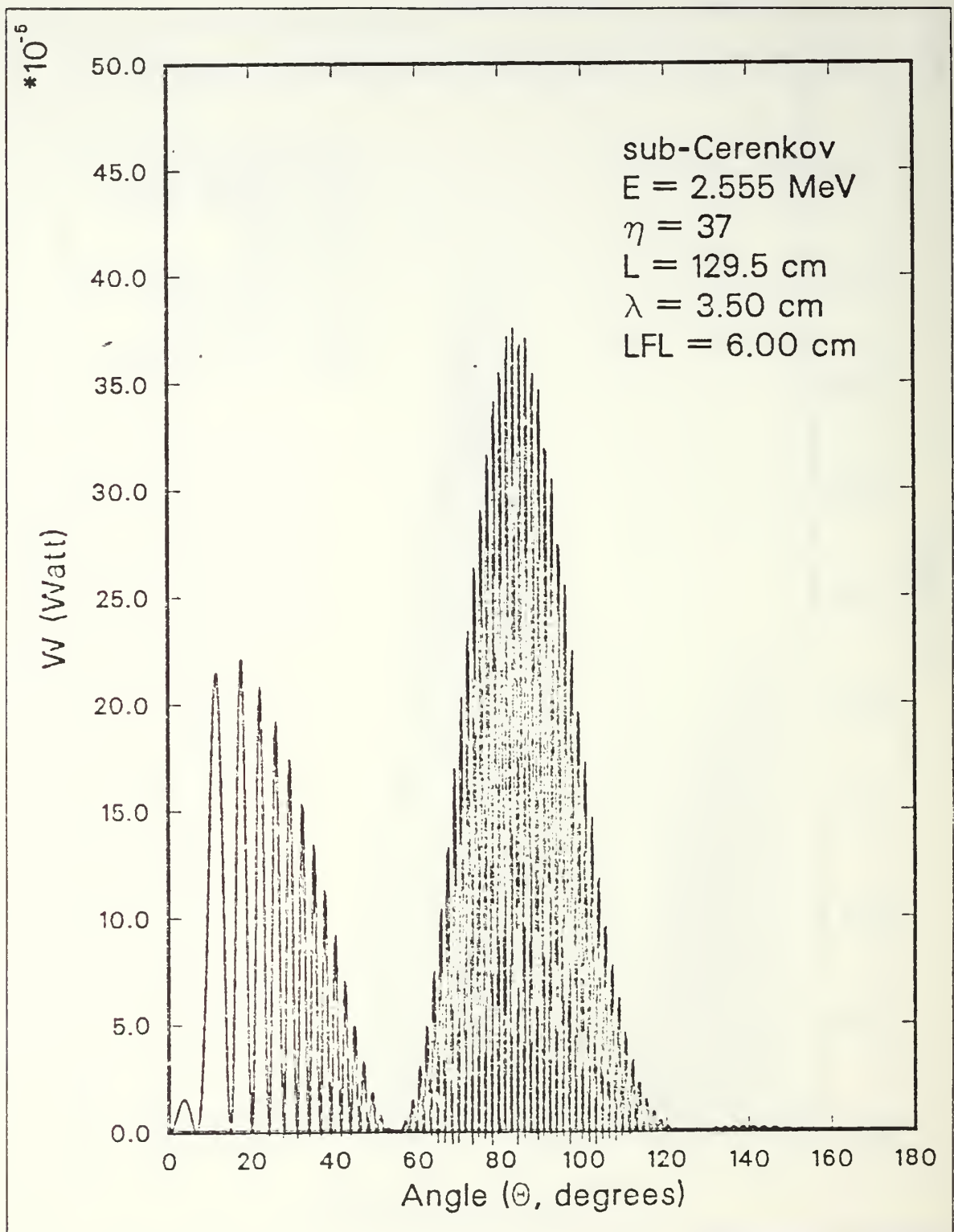


Fig. 3.20 Level Function with $LFL/\lambda = 1.71$, $\eta = 37$

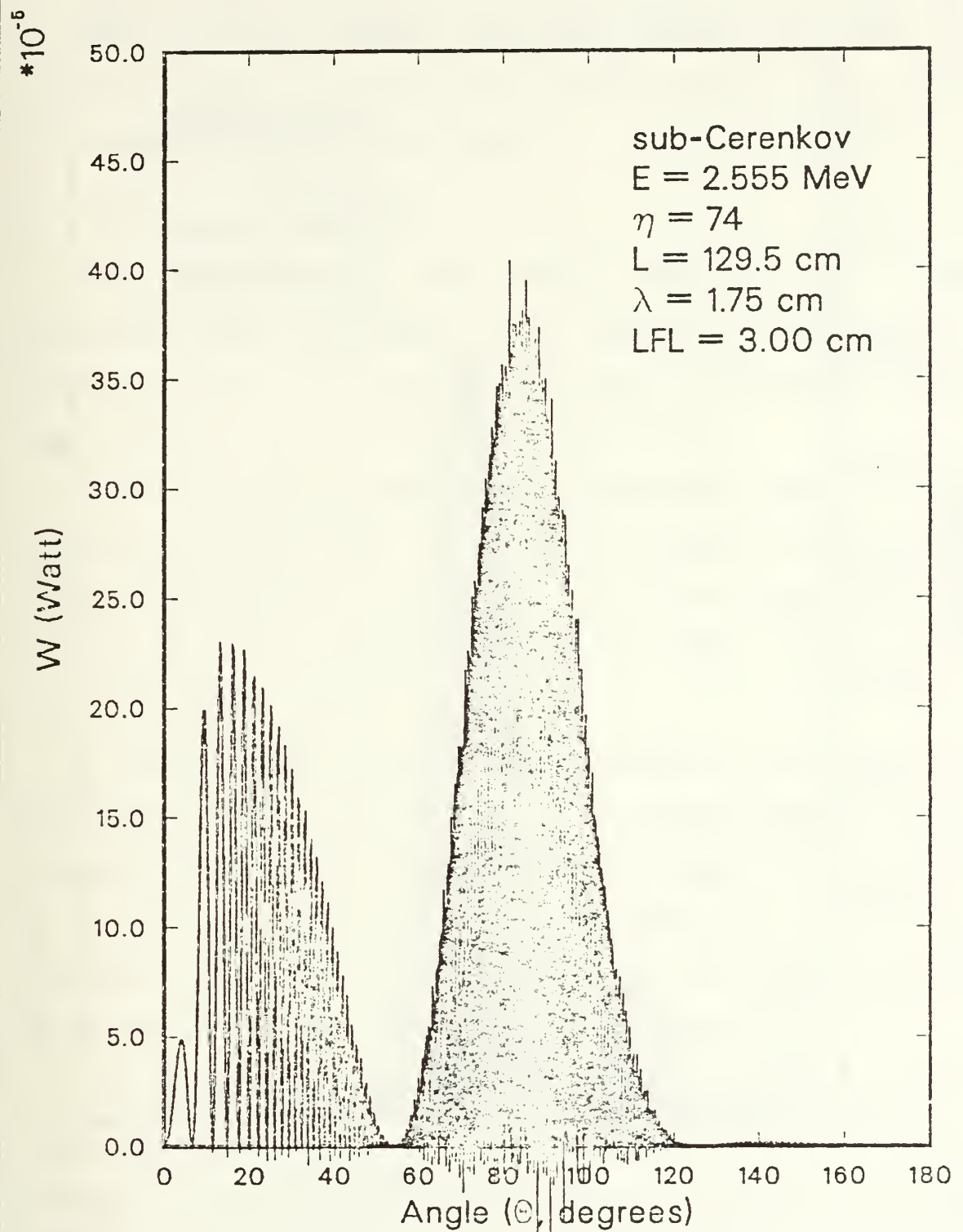


Fig. 3.21 Level Function with $LFL/\lambda = 1.71$, $\eta = 74$

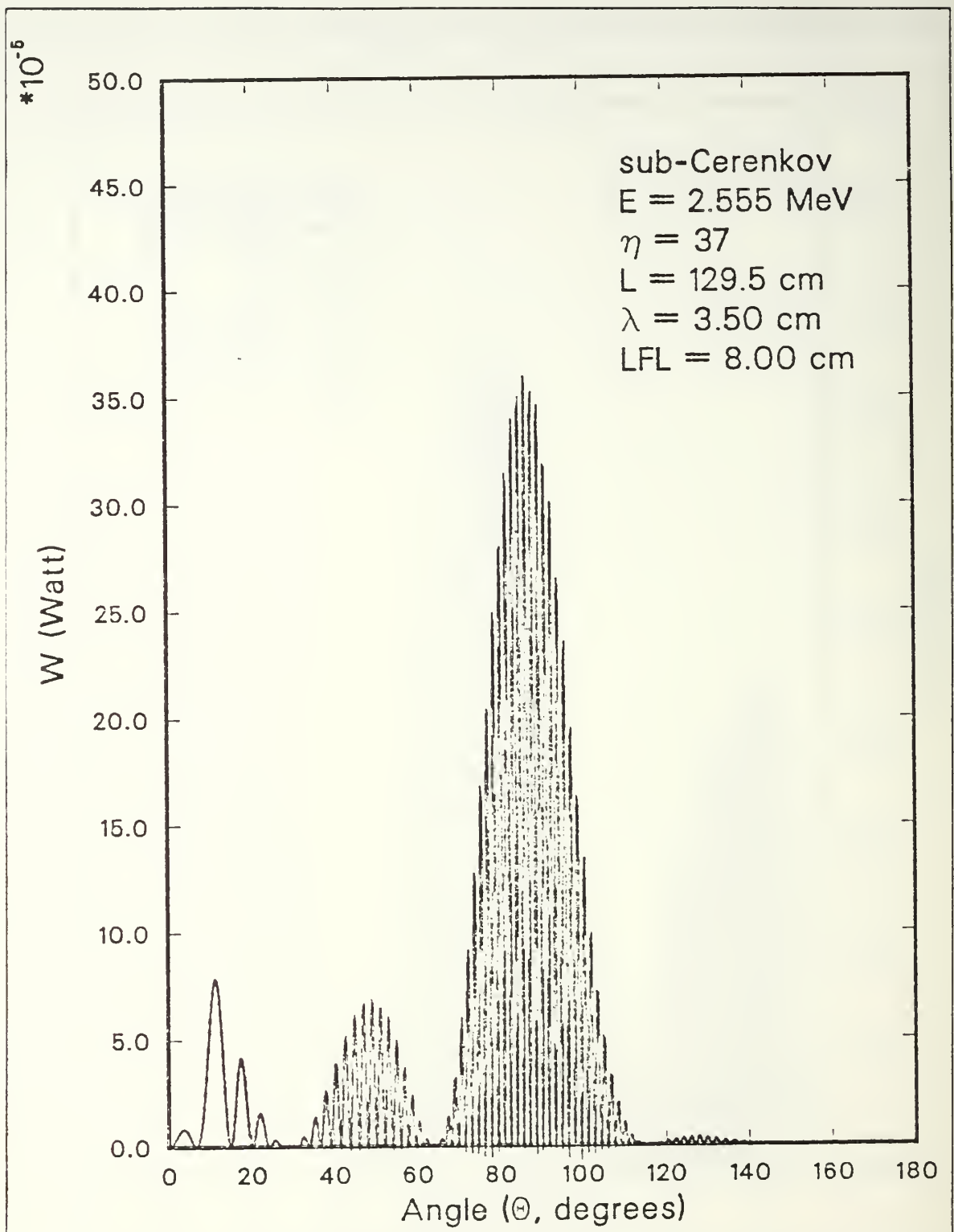


Fig. 3.22 Level Function with $LFL/\lambda = 2.28$, $\eta = 37$

Fig. 3.16 to Fig. 3.22 drawn for $\eta = 37$ show the increasing dominance of the form factor below threshold. The pattern oscillates very rapidly, but otherwise the results are as above. In fact the rapid oscillations make the form factor more evident in this series of figures.

D. TRAPEZOIDAL FUNCTION

Both the Gaussian and level function distributions have a single characteristic length; the trapezoid is more complicated in having two, the length of the base, l_b , and the length of the top, l_t . In the fourier transform these appear as $\ell = (l_b + l_t)/2$ and $l = (l_b - l_t)/2$.

Fig. 3.23 through 3.32 show radiation patterns for a trapezoidal charge distribution for different values of top and base lengths. All except the last three, Fig. 3.30 through Fig. 3.32 are for $\eta = 12$. TFTL is the symbol for the top level length of the trapezoidal function and TFBL, for the base level length of trapezoidal function.

As mentioned earlier, the form factor is sensitive to the ratios of the characteristic lengths to the wavelength of the emitted radiation. Here the appropriate ratios are ℓ/η and l/λ . In Fig. 3.23 both these ratios are less than one so that the radiation pattern is characteristic of a point charge distribution. Fig. 3.24 drawn for $\ell/\lambda = 1.2$ and $l/\lambda = 0.29$ shows a different pattern with the form factor already becoming quite evident.

Fig. 3.25 through Fig. 3.27, calculated for a constant slightly larger ratio of $\ell/\lambda = 1.71$, and increasing values of l/λ are all similar since the radiation wavelength is too large to be sensitive to the smaller details of the charge distribution. The same comment applies also to Fig. 3.28 for which ℓ/λ is still larger but l/λ is less than one.

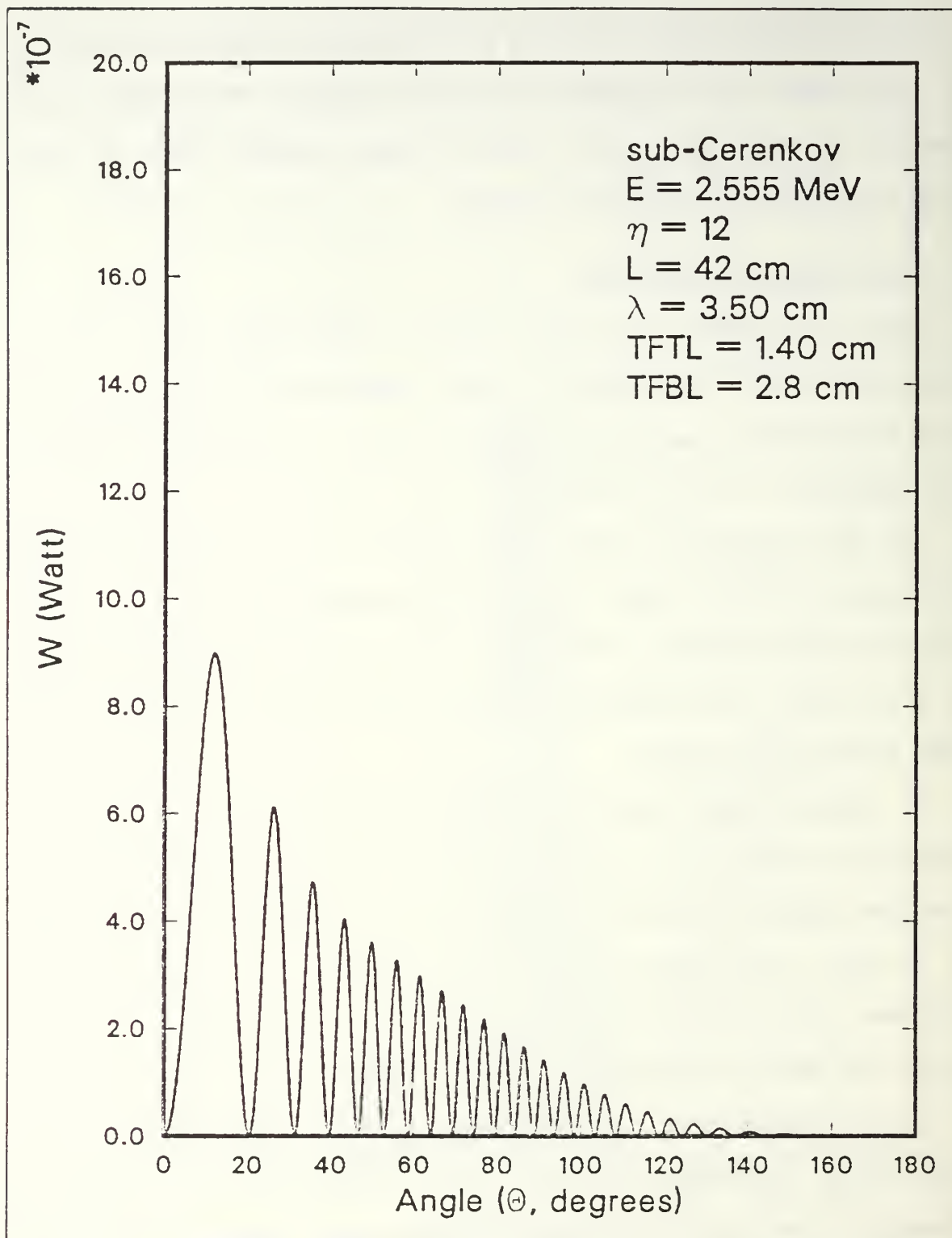


Fig. 3.23 Trapezoidal Function with $\ell/\lambda = 0.60$, $1/\lambda = 0.20$

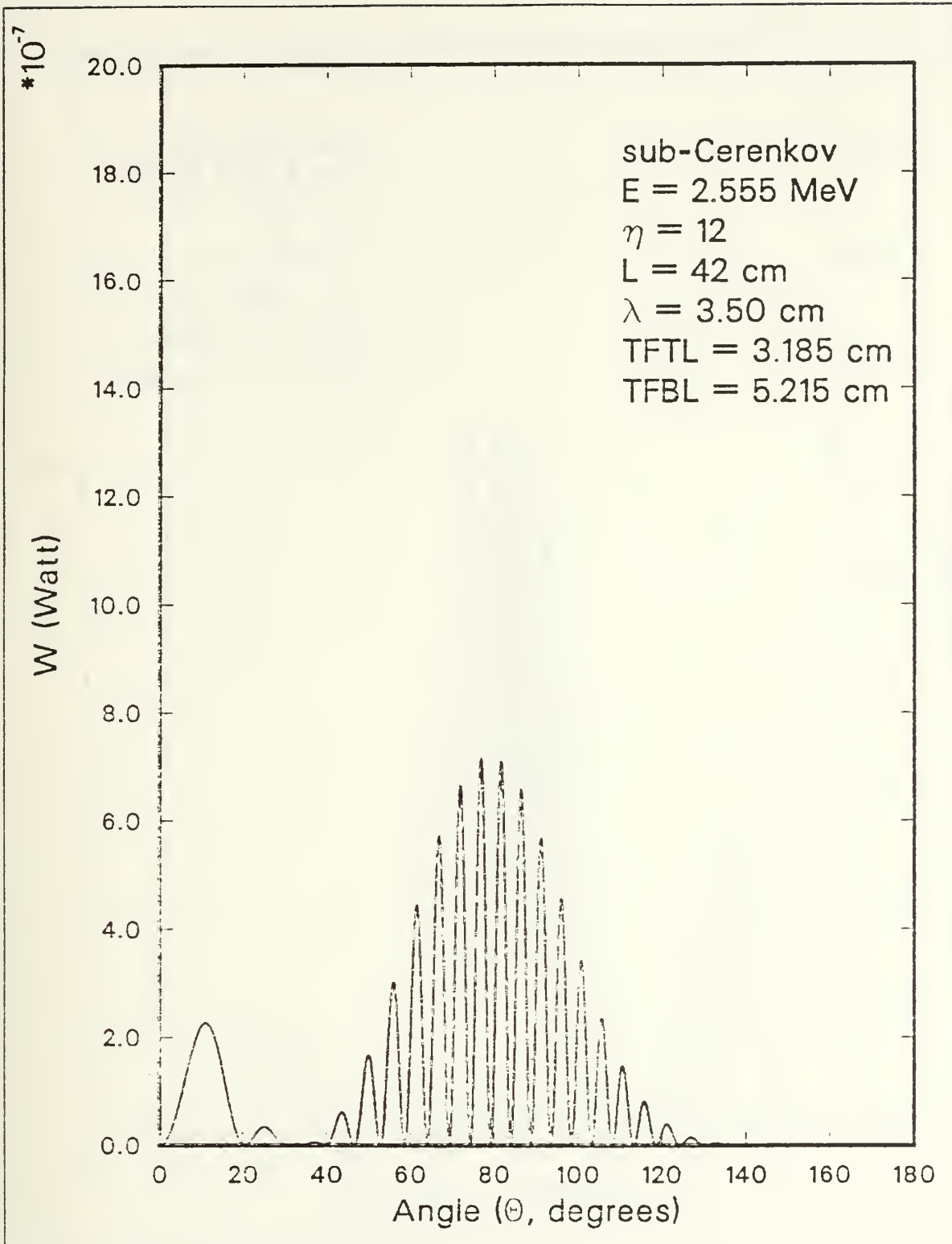


Fig. 3.24 Trapezoidal Function with $\ell/\lambda = 1.20$, $1/\lambda = 0.29$

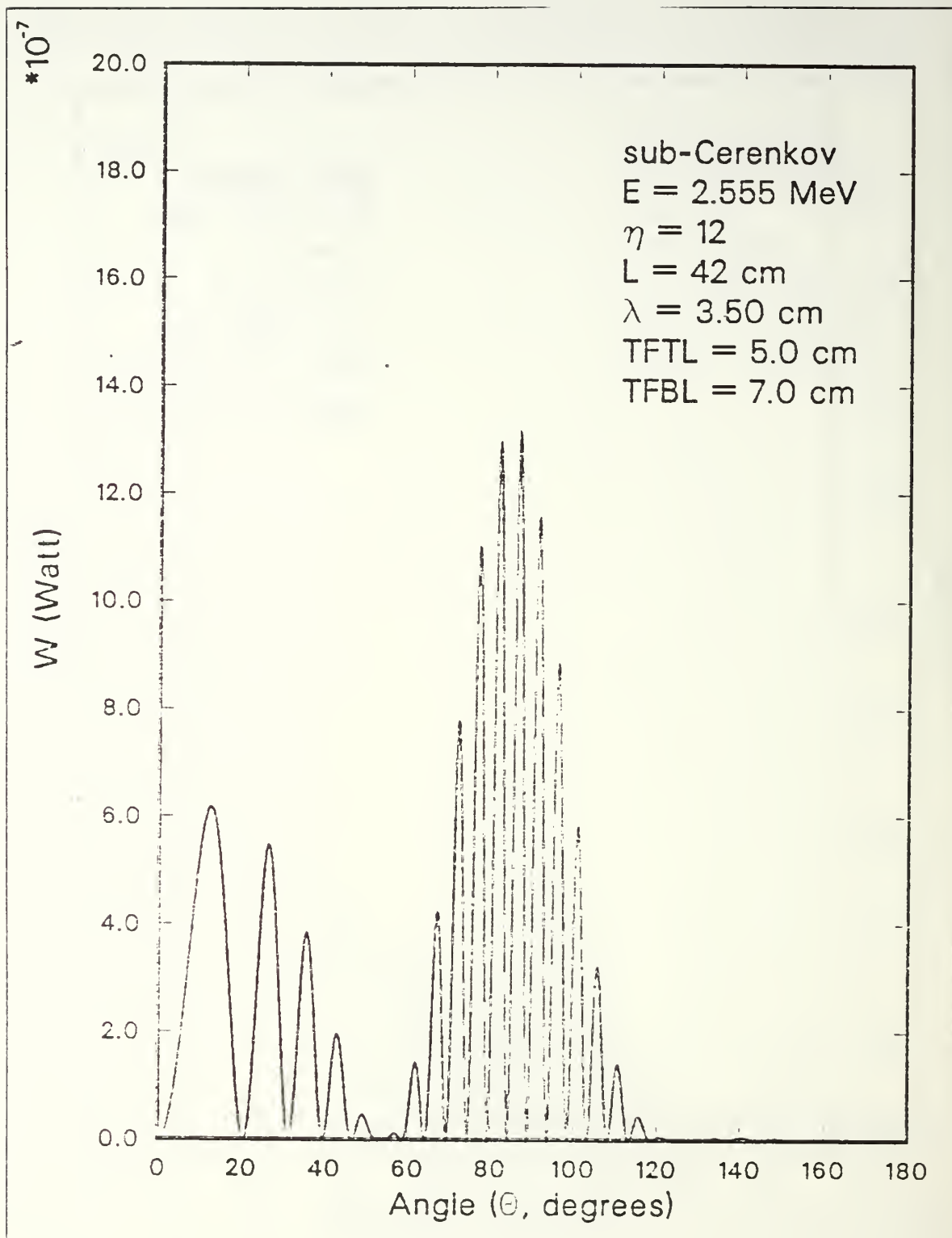


Fig. 3.25 Trapezoidal Function with $l/\lambda = 1.71$, $1/\lambda = 0.29$

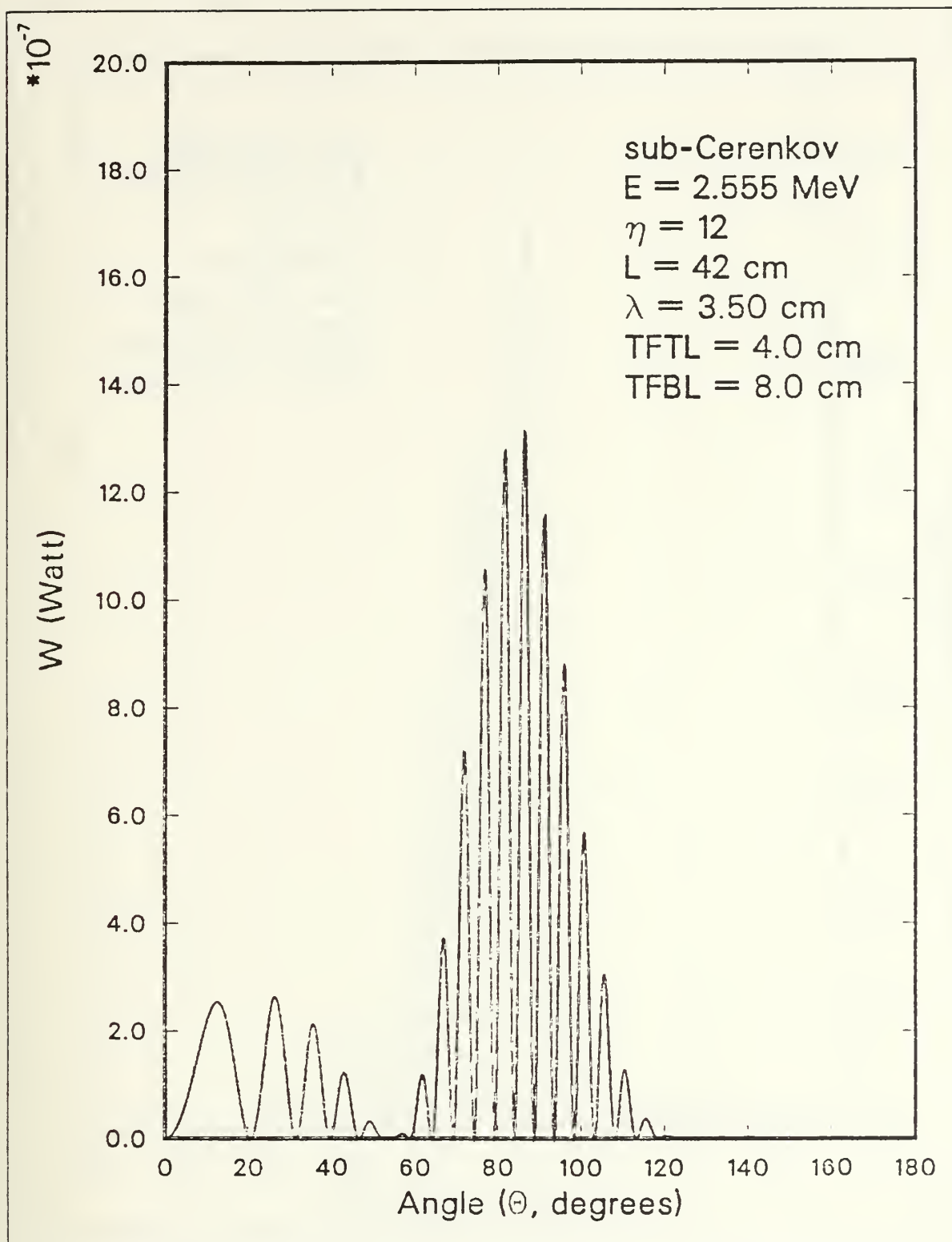


Fig. 3.26 Trapezoidal Function with $\ell/\lambda = 1.71$, $1/\lambda = 0.57$

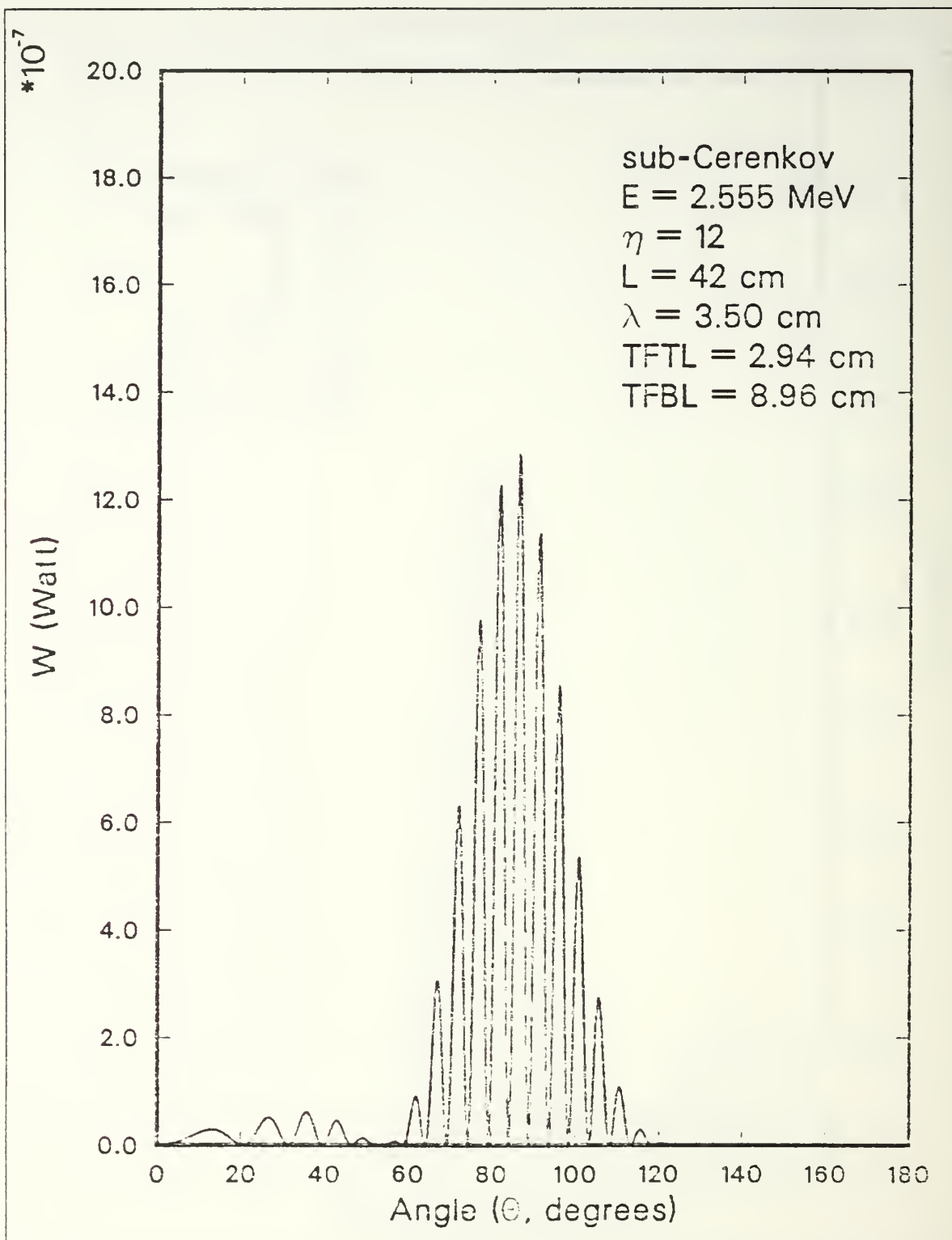


Fig. 3.27 Trapezoidal Function with $\ell/\lambda = 1.71$, $1/\lambda = 0.86$

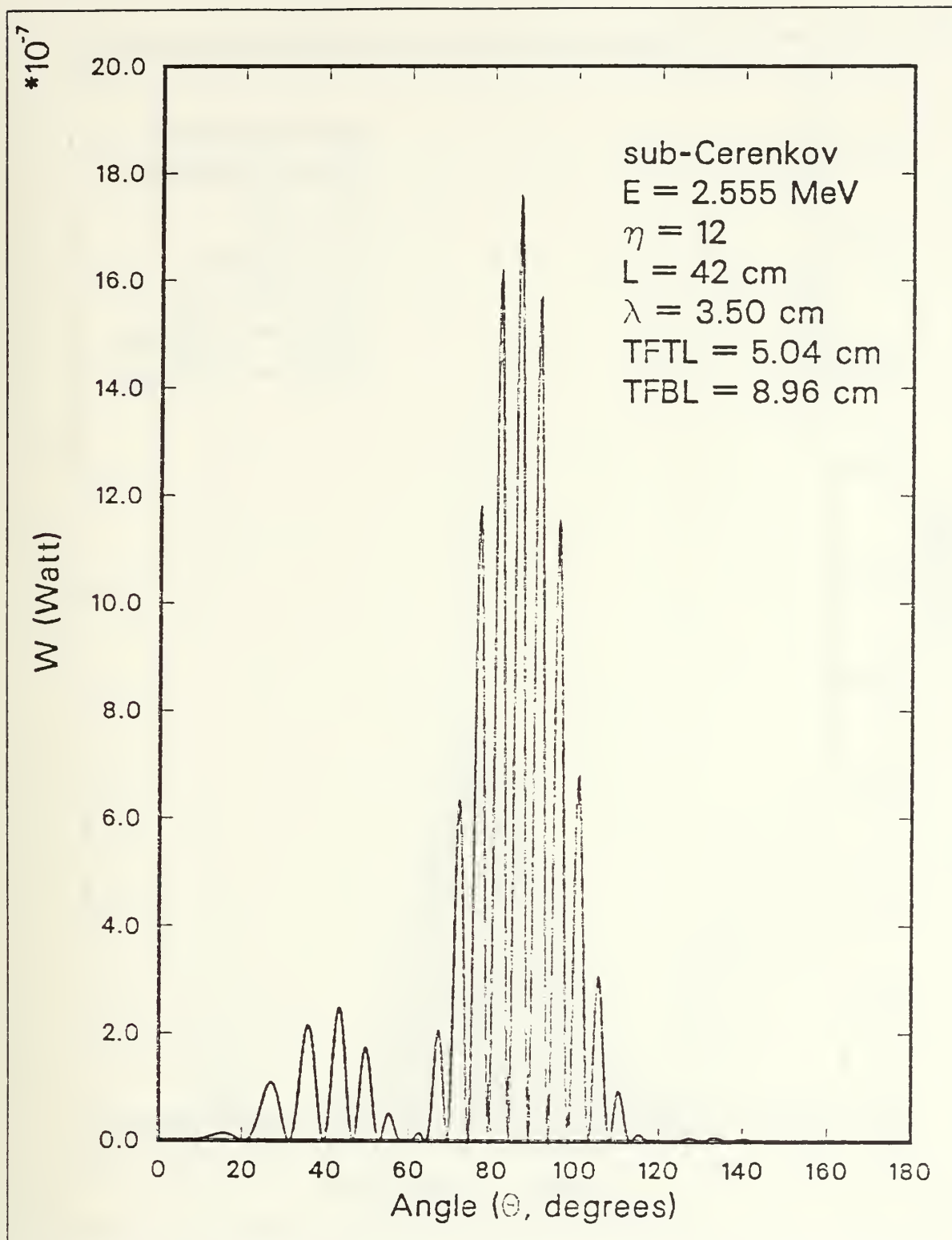


Fig. 3.28 Trapezoidal Function with $\ell/\lambda = 2.00$, $1/\lambda = 0.56$

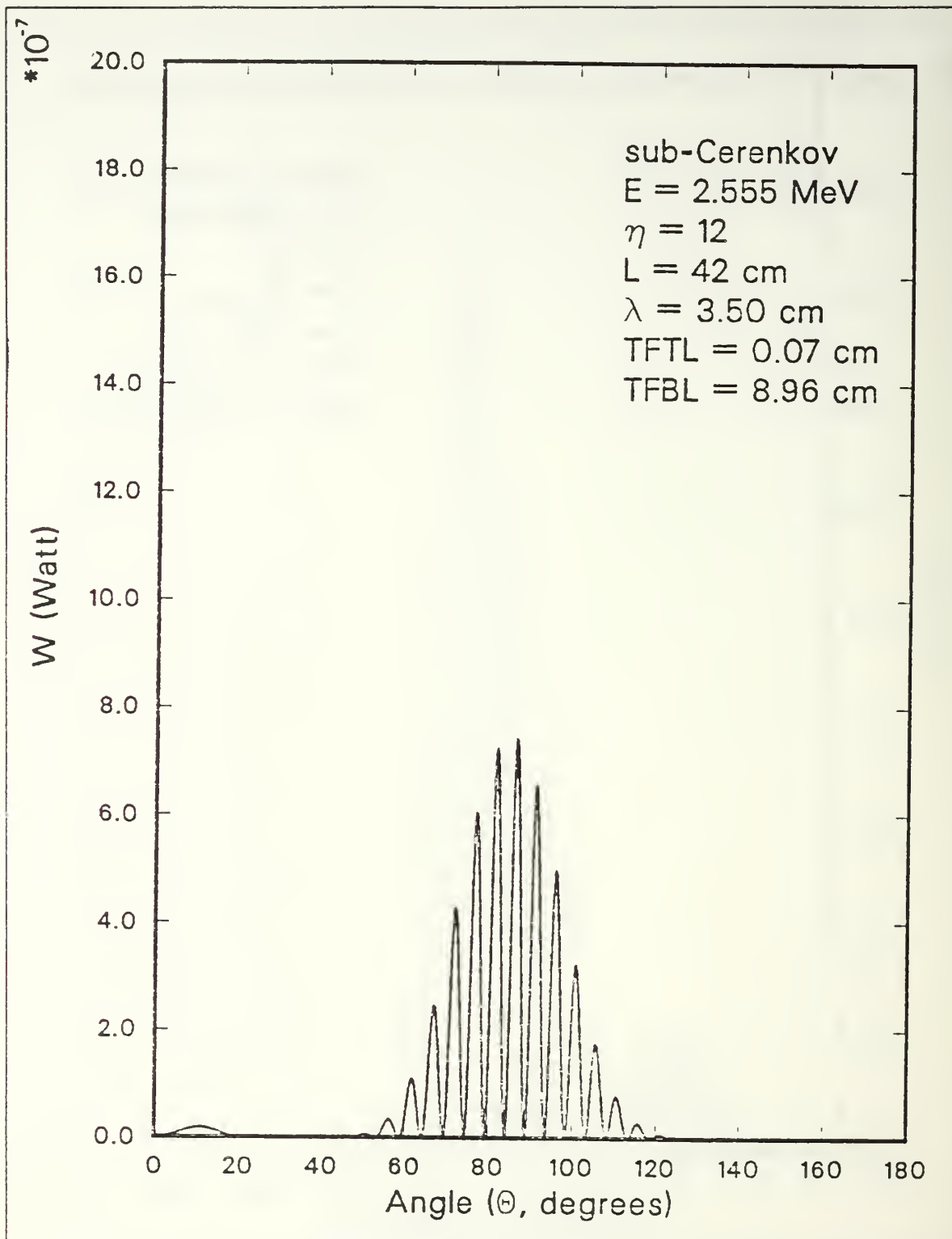


Fig. 3.29 Trapezoidal Function with $\ell/\lambda = 1.29$, $1/\lambda = 1.27$

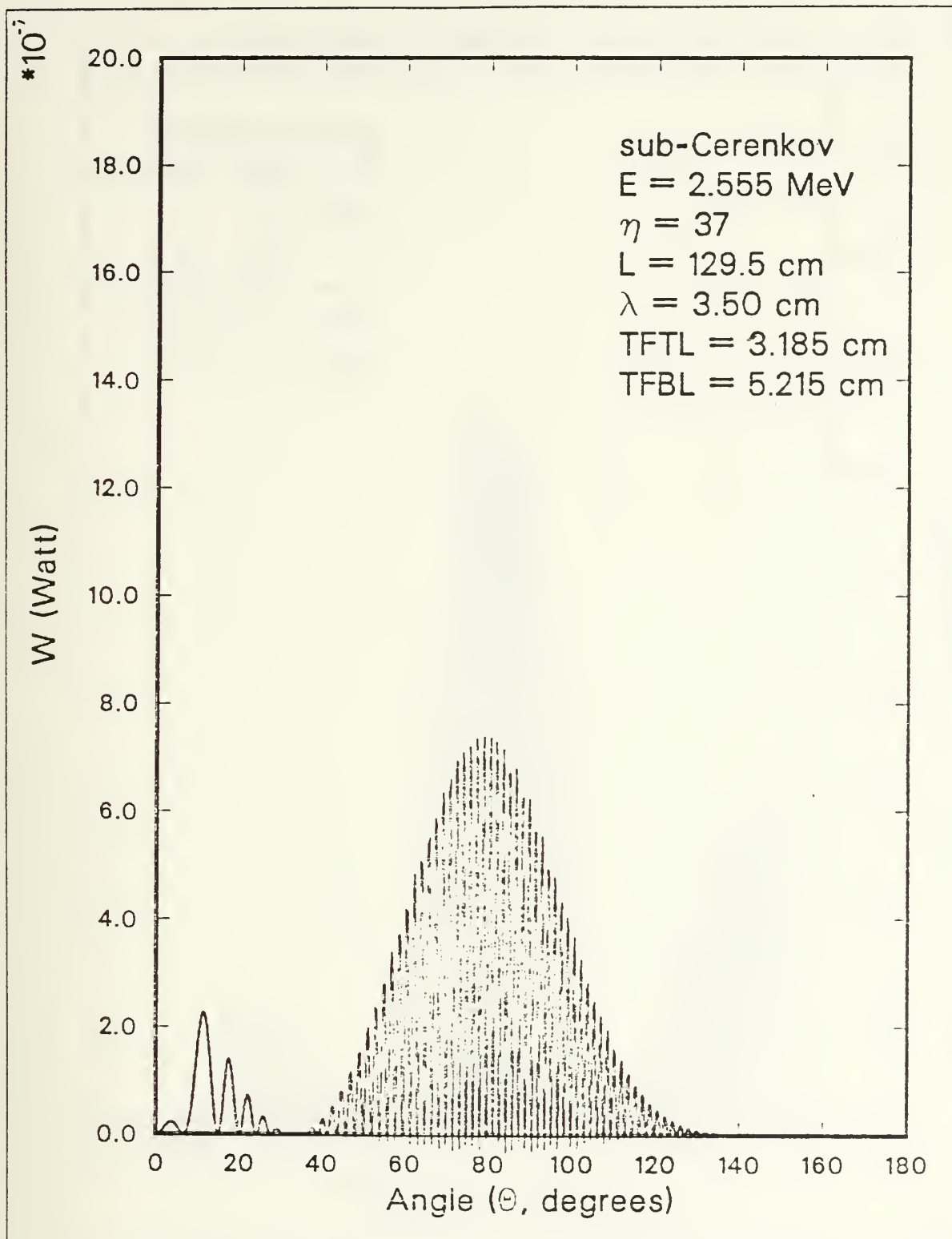


Fig. 3.30 Trapezoidal Function with $\ell/\lambda = 1.20$, $1/\lambda = 0.29$

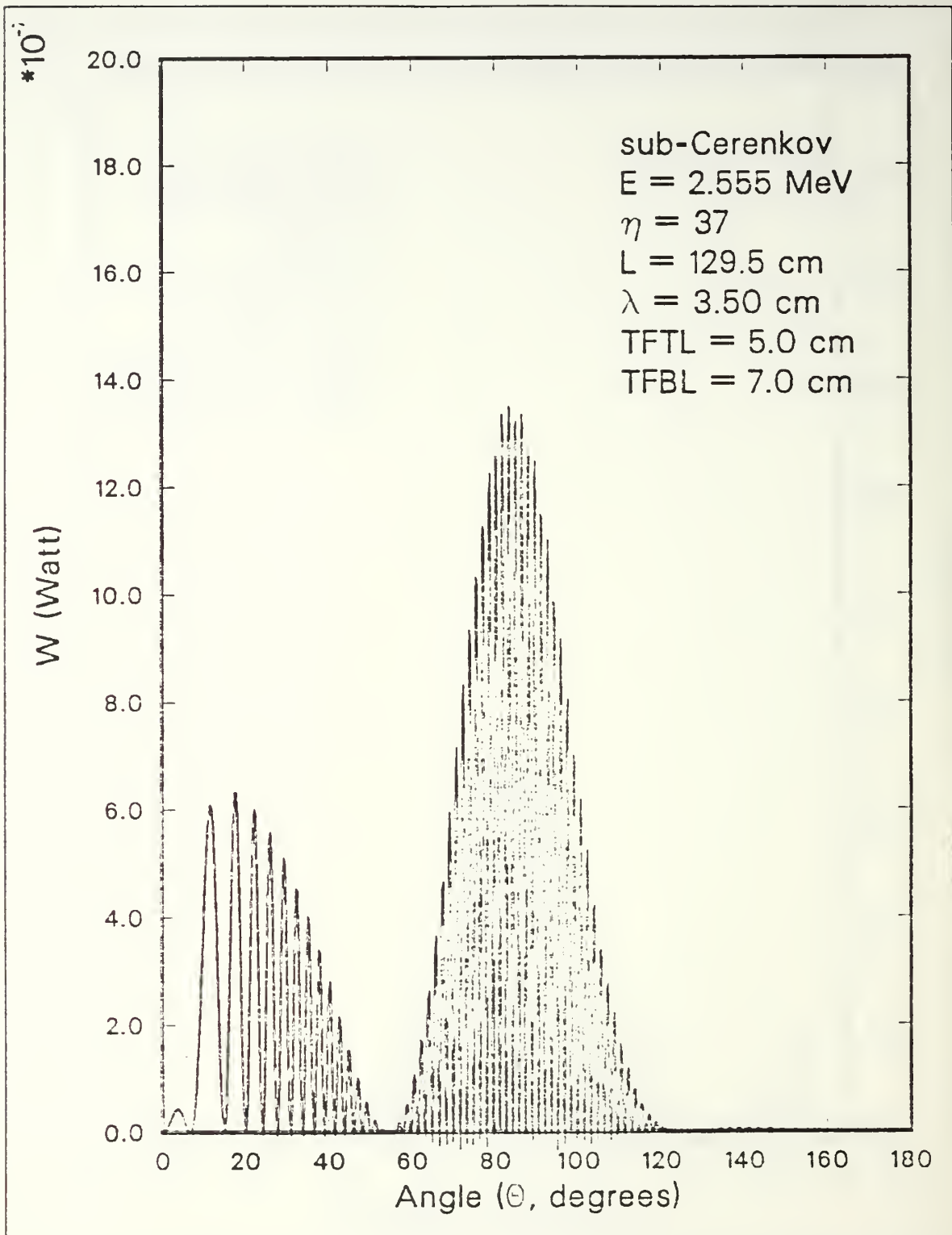


Fig. 3.31 Trapezoidal Function with $\ell/\lambda = 1.71$, $1/\lambda = 0.29$

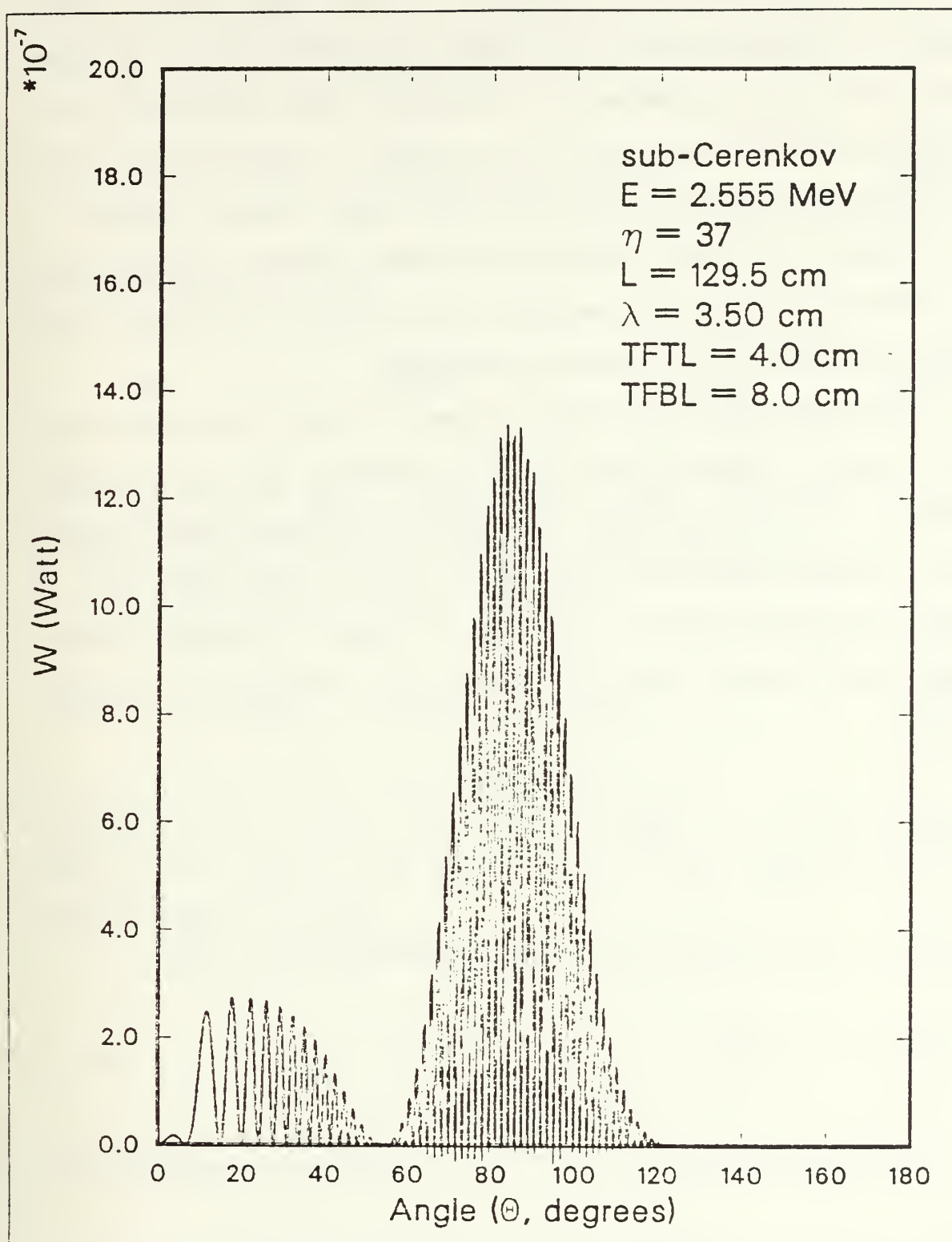


Fig. 3.32 Trapezoidal Function with $\ell/\lambda = 1.71$, $1/\lambda = 0.57$

The last figure of the $\eta = 12$ series is drawn for both ℓ/λ and l/λ greater than one. Consequently one would expect the radiation envelope to display both terms in the form factors for a trapezoidal charge distribution. That it apparently does not may be due to the fact that the lengths chosen in order to achieve these make for a charge distribution which is almost triangular.

Figures 3.30–3.32 are calculated for the below threshold condition of $\eta = 37$. All have ℓ/λ greater than one and l/λ less than one. As with other figures with this value of η , the envelope is more evident.

When both values of ℓ/λ and l/λ increase the peak values decrease mainly in the region of angles between 0° and approximately 55° and the radiation intensity is enhanced around 90° . It is difficult to determine the development of the radiation pattern with respect to ℓ/λ and l/λ because both values can change the radiation pattern at same time. To analyze the radiation pattern in another way the angle where zeros happen can be investigated by calculation. Let's set:

$$\frac{k_z \ell}{2} = n \pi, \quad \frac{k_z l}{2} = m \pi \quad (3.1)$$

where $k_z = k \cos \theta$, and m, n are integers. Substituting for k_z gives

$$\cos \theta_n = \pm n \frac{\lambda}{\ell}, \quad \cos \theta_m = \pm m \frac{\lambda}{l} \quad (3.2)$$

If as in most cases considered here $\frac{l}{\lambda} < 1$, these are no solutions for θ_m .

Thus only the solutions for θ_n are considered below. A example is Fig. 3.25 where $\frac{\ell}{\lambda} = 1.71$, $\ell = 6$ cm, $\lambda = 3.5$ cm.

$$\cos \theta = \pm n \frac{3.5}{6} = \pm n \frac{1}{1.71} = \pm n \times 0.58 \quad (3.3)$$

The solutions are for θ_n are

$$\theta_1 = 54.5^\circ \text{ and } \theta_{-1} = 125.5^\circ. \quad (3.4)$$

which agree with the figure. These values also apply to Fig. 3.26, Fig. 3.27, Fig. 3.31, and Fig. 3.32 which have the same ratio of $\frac{\ell}{\lambda}$.

In Fig. 3.29 where $\frac{\ell}{\lambda} = 1.29$, $1/\lambda = 1.27$,

$$\cos \theta_n = \pm n \frac{1}{1.29}, \quad \cos \theta_m = \pm m \frac{1}{1.27} \quad (3.5)$$

The solutions are $\theta_1 = 39.2^\circ$, $\theta_{-1} = 129.2^\circ$ for θ_n and $\theta_1 = 38^\circ$, $\theta_{-1} = 128^\circ$. In This case the zeros for θ_m and θ_n are so close together as to be indistinguishable in the figure.

IV. CONCLUSIONS AND RECOMMENDATIONS

The object of this work is to assess the effects of the charge distribution of a bunch on the sub-Cerenkov radiation from a charged particle beam, specifically investigating the short beam path region at energies above and below the threshold. It contains many calculated radiation patterns for the three kinds of charge distributions.

With the charge distribution of Gaussian function, the radiation intensity envelope near 90° represents the square of the bunch form factor $F(k)$ when the bunch length is larger than a half of the wavelength. When the bunch length is about same as the wavelength or larger than that of the level charge distribution the radiation pattern around 90° is also dominated by the square of the bunch form factor $F(k)$.

It is difficult to determine the characteristics of the radiation pattern on the trapezoidal function by the ratio of bunch length to wavelength because the level top length and level base length can change the shape of radiation pattern at same time. However the radiation pattern of the trapezoidal function can be partially characterized by analyzing the zeros of the curves.

A summary of results is :

1. When the bunch length is much smaller than the wavelength of the emitted radiation, the radiation pattern is characteristic of point charge.
2. When η is increased the total radiation pattern does not change except for minor differences in the frequency of oscillation.

3. When the wavelength of the emitted radiation is comparable to or larger than the bunch length, a significant amount of radiation appears at near 90° to the beam.
4. The envelope of the 90° radiation is the square of the bunch form factor. This envelope is skewed slightly as a result of monotonic character of the geometrical envelope function.

To enhance this preliminary work the following is recommended:

1. Investigate the behavior of the square of form factor $F(k)$ only when the bunch length varies. This will give the insight into the behavior of radiation pattern.
2. Determine why varying the top length of the trapezoidal pulse shape causes significant enhancement of the forward lobe envelope.
3. Determine the effects of changes in beam energy, pulse width, pulse frequency, and path length.
4. Confirm the results found by mapping the microwave radiation measured at a comparable particle accelerator.

The examples presented here are idealized and there has been no attempt to take into consideration such factors as beam pulse erosion as it transverses the atmosphere and the ground plane reflection in interference[Ref. 4: p.1996]. But the complete angular map of the envelope of the radiation pattern could provide a measure of $F(k_z)$ and an excellent reference to establish a method of determining the beam pulse charge distribution based on sub-Cerenkov radiation patterns.

APPENDIX A

PROGRAM FOR CALCULATION OF RADIATED POWER

```
*****
* THIS PROGRAM IS TO CALCULATE THE POWER PER UNIT SOLID ANGLE RADIA- *
* TED AT THE FREQUENCY NU. IT WAS ORIGINALLY DEVELOPED BY PROFESSOR *
* JOHN R. NEIGHBOURS AND OTHERS FOR TECTRONIX COMPUTER. THIS AUTHOR *
* MODIFIED TO RUN ON IBM 370 MAINFRAME COMPUTER IN DEC. 1987.      *
* THE THEORY AND ALL EQUATION ARE WELL GIVEN IN REF. 5.           *
*****
```

```
PROGRAM JNN
COMMON /VA/HH,HU,SDXX /DOUPA/L,ETA,TMAX,DT,E,N,B,LL,RR,NN,RFTL,
+      RFBL,TFTL,TFBL,TRIBL,NBETA
DOUBLE PRECISION C,C0,MU0,NU0,Q,PI,E0,E,NBETA,
DOUBLE PRECISION TMAX,DT,NU,L,ETA,N,B,LL,RR,NN
DOUBLE PRECISION IIMAX,KK,CONST,WMAX,THETA,W,T,KKZ,H,DENOM1,
DOUBLE PRECISION DENOM2,K0
DOUBLE PRECISION GAMMA,V,U,II,R,HA,HB,HC,HD,DD,DEXIN
DOUBLE PRECISION RFTL,RFBL,TFTL,TFBL,TRIBL
DOUBLE PRECISION DENOM3,DENOM4,DENOM5,DENOM6,DENOM7,DENOM8,
DOUBLE PRECISION HE,HF,HG,HI
DOUBLE PRECISION HJ,HK,HL,Z,LI,LIN,HX,HW,KE,SDXX
REAL XWMAX,XTHETA,XW,YMAX,SDYY,SDY,JX,JYY,YY,YNUM,X,Y,SDX,
+      XX ,XNUM,RTMAX,RSDXX,RWMAX,RTHETA,RW
REAL REL,REE,REN,REB,RELL,RERR,RENN,DELTA
REAL RERFTL,RERFBL,RETFTL,RETFBL,RETRIB,REHU
INTEGER I,K,KMAX,IMAX,HH,J,JXMAX,JYMAX,IPA,P,HU
CHARACTER*1 PARACH,EXPPTS,EXPTCH,SAVEQ,PPRE,CHANGE,ANS,AXCH,
+      ANS2,ANS3
CHARACTER*13 NAMEPF,NAMEWF,NAMEEX
DIMENSION XTHETA(1:100)
DIMENSION XW(1:100)
DIMENSION THETA(0:4500)
DIMENSION W(0:4500)
DIMENSION H(1:7)
```

C

C

C

```
* ASSIGNMENT OF CONSTANTS
```

```
C=2.997122D08
```

```
C0=2.997925D08
```

```
MU0=1.2566437061D-06
```

C

C

C

```
***** TO VARY CHARGE *****
```

```
PI=3.1415926535897932D0
```

```

      E0=0.5117D0
C
5    PRINT*, '
      PRINT*, ' ENTER BUNCH CHARGE.(DEFAULT= 1.5E-12) '
      READ*, Q
      IF(Q.GT.0) GO TO 45
      Q=1.5D-12
45   PRINT*, ' ENTER FUNDAMENTAL FREQUENCY NU0. (DEFAULT= 2.85E9)'
      READ*, NU0
      IF(NU0.GT.0) GO TO 55
      NU0=2.85D09
55   CONTINUE
C
      PRINT*, 'THE INDEX OF REFRACTION IN THE AIR IS 1.000268(DEFAULT).'0
      PRINT*, 'DO YOU WISH TO CHANGE? (Y/N) '
      READ '(1A)', ANS2
      IF(ANS2.EQ.'Y') THEN
        PRINT*, 'ENTER THE INDEX OF REFRACTION. '
        READ*, DEXIN
      ELSE
        DEXIN=1.000268D0
      END IF
      C=C0/DEXIN
C
C ***** DECISION OF PARAMETER FILE*****
C
      PRINT *
      PRINT *, '      1: CREATE NEW PARAMETER FILE'
      PRINT *, '      2: USE OLD FILE'
      PRINT *, '      3: EXIT'
      PRINT *
      PRINT *, '      ENTER YOUR CHOICE :'
      READ '(1A)', PARACH
      IF(PARACH.EQ.'3') GOTO 700
      IF(PARACH.EQ.'2') CALL INAMPF
      IF(PARACH.EQ.'1') CALL MAKEPF
C
*****
*      READ IN ALL PARAMETERS FROM EXTERNAL      *
*      FILE/PRINTOUT PARAMETERS                  *
*****
C
99   WRITE(6,100)
100  FORMAT(///'THE PARAMETERS YOU ENTERED ARE:')
      REWIND 1
120  READ(1,*) HH
131  WRITE(6,135) HH
135  FORMAT(/'FOURIER TRANSFORM CHOICE :      ',I8)
      IF (HH.NE.1) GOTO 137
      WRITE (6,136)
136  FORMAT(/,37X,'GAUSSIAN FUNCTION ' )
137  IF (HH.NE.2) GOTO 139

```

```

        WRITE (6,138)
138     FORMAT (/ ,37X, 'LEVEL FUNCTION ' )
139     IF (HH.NE.3) GOTO 141
        WRITE (6,140)
140     FORMAT (/ 'SUM OF LEVEL AND RIPPLE FUNCTIONS' )
141     IF (HH.NE.4) GOTO 143
        WRITE (6,142)
142     FORMAT (/ 'MULTIPLE HUMP FUNCTION' )
143     IF (HH.NE.5) GOTO 145
        WRITE (6,144)
144     FORMAT (/ 'ROUNDED FUNCTION' )
145     IF (HH.NE.6) GOTO 147
        WRITE (6,146)
146     FORMAT (/ 'TRAPEZOIDAL FUNCTION' )
147     IF (HH.NE.7) GOTO 149
        WRITE (6,148)
148     FORMAT (/ 'TRIANGLE FUNCTION' )
C
149     READ(1,*) ETA
9151    WRITE(6,151) ETA
151     FORMAT (/ '    ETA (L/RAMMDA) :                ',D16.4)
        READ(1,*) TMAX
154     WRITE(6,155) TMAX
155     FORMAT (/ '    MAXIMUM THETA VALUE :                ',D16.4)
        READ(1,*) DT
164     WRITE(6,165) DT
165     FORMAT (/ '    THETA CALCULATION INCREMENT : ',D16.4)
        READ(1,*) SDXX
174     WRITE(6,175) SDXX
175     FORMAT (/ '    THETA MARKING INCREMENT :          ',D16.4)
C
        READ(1,*) E
        READ(1,*) NBETA
C184    WRITE(6,185) E
184     WRITE(6,185) NBETA
C185    FORMAT (/ '    BEAM ENERGY :                ',D16.4)
185     FORMAT (/ '    VALUE OF NBETA :                ',D16.4)
        READ(1,*) N
194     WRITE(6,195) N
195     FORMAT (/ '    HARMONIC NUMBER :                ',D16.4)
C
C
        IF (HH.NE.1) GOTO 206
C
        READ(1,*) B
204     WRITE(6,205) B
205     FORMAT (/ '    BUNCH LENGTH (M) :                ',D16.4)
C
206     IF (HH.LT.2) GOTO 216
        IF (HH.GT.4) GOTO 216
C
        READ(1,*) LL
214     WRITE(6,215) LL

```

```

215  FORMAT(/'    LEVEL FUNCTION LENGTH (M) :          ',D16.4)
C
216  IF (HH.NE.3) GOTO 9235
C
      READ(1,*) RR
224  WRITE(6,225) RR
225  FORMAT(/'    FOURIER RATIO CONSTANT :          ',D16.4)
C
C
      READ(1,*) NN
234  WRITE(6,235) NN
235  FORMAT(/'    NUMBER OF RIPPLES :                ',D16.4)
C
9235  IF (HH.NE.4) GOTO 236
C
      READ (1,*)HU
9237  WRITE (6,9239) HU
9239  FORMAT(/'    NUMBER OF HUMPS :                  ',I4)
C
236  IF (HH.NE.5) GOTO 241
C
      READ (1,*) RFTL
9238  WRITE (6,238) RFTL
238  FORMAT (/ '    ROUNDED FUNCTION LEVEL TOP LENGTH :      ',D16.4)
C
      READ (1,*) RFBL
9240  WRITE (6,240) RFBL
240  FORMAT (/ '    ROUNDED FUNCTION BASE LENGTH :          ',D16.4)
C
241  IF (HH.NE.6) GOTO 246
C
      READ (1,*) TFTL
9243  WRITE (6,243)TFTL
243  FORMAT (/ '    TRAPEZOIDAL FUNCTION TOP LEVEL LENGTH : ',D16.4)
C
      READ (1,*) TFBL
9245  WRITE (6,245)TFBL
245  FORMAT (/ '    TRAPEZOIDAL FUNCTION BASE LENGTH :      ',D16.4)
C
246  IF (HH.NE.7) GOTO 249
C
      READ (1,*) TRIBL
9248  WRITE (6,248)TRIBL
248  FORMAT (/ '    TRIANGLE FUNCTION BASE LENGTH :          ',D16.4)
249  WRITE(6,250)
250  FORMAT(// 'DO YOU WISH TO CHANGE ANY OF THESE ?(Y OR N)')
      READ'(A1)', CHANGE
C
      IF(CHANGE.EQ.'Y') GO TO 700
C
*****
* *** BEGIN CALCULATION *** *

```

```

C
325  IIMAX=TMAX/DT
      IMAX=INT( IIMAX)
      NU=N*NU0
      IF ((HH.GE.2).AND.(HH.LE.4)) THEN
        DD=LL/2.0D0
      END IF
C
      KK=2.0D0*PI*NU/C
      CONST=MU0*C*(NU0**2.0)*(Q**2.0)/(8.0D0*(PI**2.0))
      WMAX=0.0D0
      DO 350 I=0,IMAX
        THETA(I)=DBLE(I)*DT
        T=PI*THETA(I)/180.0D0
        KKZ=KK*DCOS(T)
C
        IF (HH.NE.1) GOTO 326
C
        H(1)=DEXP(-1.0D0*((KKZ*B/2.0D0)**2.0))
C
326  CONTINUE
      IF (HH.LT.2) GOTO 328
      IF (HH.GT.3) GOTO 328
C
      DENOM1=KKZ*DD
      IF (DENOM1.EQ.0) GOTO 327
      H(2)=(DSIN (KKZ*DD))/(KKZ*DD)
      GOTO 328
327  H(2)=0.0D0
C
328  IF(HH.NE.3) GOTO 333
C
      KO=PI*NN/DD
      DENOM2=(KKZ-KO)*DD
C
      IF(DENOM2.EQ.0) GOTO 329
C
      HA= DSIN(DENOM2)/DENOM2
C
      GOTO 330
C
329  HA=0.0D0
330  DENOM3=(KKZ+KO)*DD
C
      IF (DENOM3.EQ.0) GOTO 331
C
      HB=DSIN(DENOM3)/DENOM3
C
      GOTO 332
C
331  HB=0.0D0

```

```

332      H(3)=H(2)+((RR/2.0D0)*(HA+HB))
C
333      IF(HH.NE.4) GOTO 335
C
      Z=(KKZ*DD)
C
      IF(Z.EQ.0) GOTO 334
C
      H(4)=1.0D0*((DSIN(Z))/Z)
      DENOM4= 1.0
      DO 9333 P=1,HU
        KE=(2.0D0*DBLE(P))-1.0D0
        LI=((2.0D0*DBLE(HU))-KE)/((2.0D0*DBLE(HU))-1.0D0)
        LIN=((-1.0D0)**DBLE(P))*(-1.0D0)
        HX=(LIN*LI*DSIN(Z*LI))/(Z*LI)
        HW=LIN*LI
        H(4)=H(4)+HX
        DENOM4= DENOM4+HW
9333    CONTINUE
      H(4)=H(4)/DENOM4
C
      GOTO 335
C
334      H(4)=0.0D0
C
335      IF (HH.NE.5) GO TO 339
C
      HL=(8D0*16D0)/(((RFBL-RFTL)**2.0)*(KKZ**3)*(RFBL+RFTL))
      HG=HL*DSIN((KKZ/4.0D0)*(RFBL+RFTL))
      HJ= (RFTL*DSIN(KKZ*RFTL/2.0D0))/(KKZ*RFTL/2.0D0)
      HK= (RFBL*DSIN(KKZ*RFBL/2.0D0))/(KKZ*RFBL/2.0D0)
      HI=(32D0/((((RFBL-RFTL)*(KKZ))**2.0)*(RFTL+RFBL)))*(HJ+HK)
      H(5)=HG-HI
C
339      IF (HH.NE.6) GOTO 345
C
      DENOM6=KKZ*(TFBL+TFTL)/4.0D0
      DENOM7=KKZ*(TFBL-TFTL)/4.0D0
      HE=DSIN(DENOM6)/DENOM6
      HF=DSIN(DENOM7)/DENOM7
      H(6)=(TFBL+TFTL)/2.0D0*HE*HF
C
345      IF(HH.NE.7) GOTO 349
C
      DENOM5=(KKZ*TRIBL)/4.0D0
C
      IF (DENOM5.EQ.0) GOTO 346
      H(7) = (DSIN(DENOM5)/(DENOM5))**2.0
C
      GOTO 349
C
346      H(7)=0.0D0

```

```

C
349      CONTINUE
C
C      GAMMA=E/E0
      L=ETA*C/NU
C      GAMMA=DSQRT(1.0D0/(1.0D0-(NBETA/DEXIN)**2))
C      V=C0*(DSQRT(1.0D0-(1.0D0/(GAMMA**2.0))))
      V=C0*(NBETA/DEXIN)
      U=(KK*L/2.0D0)*((C/V)-DCOS(T))
      II=DSIN(U)/U
      R=KK*L*H(HH)*II*DSIN(T)
      W(I)=CONST*(R**2.0)

C
C      *** CALCULATION OF MAXIMUM W ***
C
272      WMAX=DMAX1(WMAX,W(I))
C
350      CONTINUE
C
C      ***** DECISION TO SAVE VALUES CALCULATED *****
C
      WRITE(6,360)
360      FORMAT(/'DO WANT TO SAVE THE RESULTS IN A FILE? (Y/N)' )
      READ'(A1)', SAVEQ
C
      IF(SAVEQ.EQ.'N') GOTO 440
C
      PRINT *, 'UNDER WHAT FILE NAME? '
      READ '(A10)', NAMEWF
      OPEN(UNIT=3,FILE=NAMEWF,STATUS='NEW',FORM='FORMATTED')
      DO 370 I=0,IMAX
          RTHETA=REAL(THETA(I))
          RW=REAL(W(I))
          WRITE(3,380) RTHETA,RW
380      FORMAT(4X,F8.3,2X,F20.18)
370      CONTINUE
      WRITE(3,385)
385      FORMAT(7X,'0.000')
      WRITE(3,390) WMAX
390      FORMAT(2X,'WMAX = ',D16.4)
      WRITE(3,392) ETA
392      FORMAT(2X,'ETA = ',D16.4)
      WRITE(3,394) NBETA
394      FORMAT(2X,'NBETA = ',D16.4)
C      WRITE(3,396) B
C396      FORMAT(2X,'BUNCH LENGTH = ',D16.4)
C
C      ***** DECISION TO PRINTOUT,RE-RUN,OR EXIT *****
C
440      WRITE(6,445)
445      FORMAT(////'          1: PRINT OUT VALUES',/
+          '          2: RUN PROGRAM AGAIN',/

```

```

+          '      3: EXIT',///
+          '      ENTER CHOICE.____')
  READ'(A1)', PPRE
C
  IF(PPRE.EQ.'1') GOTO 660
  IF(PPRE.EQ.'2') GOTO 05
  IF(PPRE.EQ.'3') GOTO 700
  GOTO 440
C
C *** PRINT OUT VALUES ***
C
660  WRITE(6,670)
670  FORMAT('      THETA                W'/23('-')/ )
      DO 690 I=0,IMAX
          WRITE(6,680) THETA(I),W(I)
680  FORMAT(F8.2,F15.4)
690  CONTINUE
C
C ***** PROGRAM ENDS *****
700  END
C
C
C
C *****
* *** SUBROUTINE INAMPF *** *
*****
C
      SUBROUTINE INAMPF
C
C *** INPUT OLD PARAMETER FILE NAME
      CHARACTER*10 NAMEPF
      WRITE(6,900)
900  FORMAT('/ENTER THE NAME OF THE PARAMETER FILE YOU WISH TO',
+          ' USE(MAX 10 CHAR)  ' )
      READ'(A10)', NAMEPF
      WRITE(6,911)
911  FORMAT('/TEST LINE ONE' )
      OPEN(UNIT=1,FILE=NAMEPF,STATUS='OLD',FORM='FORMATTED',
+          BLANK='NULL' )
      WRITE(6,912)
912  FORMAT('/TEST LINE TWO' )
      RETURN
      END
C
*****
* *** SUBROUTINE INAMEX *** *
*****
C
      SUBROUTINE INAMEX
C
C *** INPUT OLD EXPERIMENTAL POINTS FILE NAME ***
      CHARACTER*10 NAMEEX

```

```

        WRITE(6,1000)
1000  FORMAT(/'ENTER NAME OF EXPERIMENTAL POINTS FILE YOU WISH',
+          'TO USE(MAX 10 CHAR) ' )
        READ'(A10)', NAMEEX
        OPEN(UNIT=2,FILE=NAMEEX,STATUS='OLD',FORM='FORMATTED',
+          BLANK='NULL' )
        RETURN
        END

C
C
*****
* *** SUBROUTINE MAKEPF *** *
*****
C
        SUBROUTINE MAKEPF
C
C      *** INPUT OF PARAMETERS INTO NEW FILE (UNIT=1)***
C
        COMMON /VA/HH,HU,SDXX /DOUPA/L,ETA,TMAX,DT,E,N,B,LL,RR,NN,RFTL,
+          RFBL,TFTL,TFBL,TRIBL,NBETA
        DOUBLE PRECISION L,ETA,TMAX,DT,E,N,B,LL,SDXX,NBETA,
+          RR,NN,RFTL,RFBL,TFTL,TFBL,TRIBL
        INTEGER HH,HU
        CHARACTER*10 NAMEPF
        WRITE(6,1300)
1300  FORMAT(/'ENTER THE NAME FOR THE NEW PARAMETER FILE.',
+          '(MAX 10 CHAR) ' )
        READ'(A10)', NAMEPF
        OPEN(UNIT=1,FILE=NAMEPF,STATUS='NEW',FORM='FORMATTED',
+          ACCESS='SEQUENTIAL',BLANK='NULL')
        PRINT*, ' '
        WRITE(6,1320)
1320  FORMAT(///// 'NOTE: ALL THE PARAMETERS MUST BE ENTERED',
+          ' ALTHOUGH SOME MAY NOT BE USED')
        WRITE(6,1330)
1330  FORMAT(/'      1: GAUSSIAN FUNCTION'/'      2: LEVEL FUNCTION',
+          '/'      3: SUM OF LEVEL AND RIPPLE FUNCTIONS',
+          '/'      4: MULTIPLE HUMP FUNCTION',
+          '/'      5: ROUNDED FUNCTION',
+          '/'      6: TRAPEZOID FUNCTION',
+          '/'      7: TRIANGLE FUNCTION')
        WRITE(6,1340)
1340  FORMAT(/'ENTER THE FOURIERTRANSFORM CHOICE:')
        READ*, HH
C
C
1356  IF(HH.LE.7) GO TO 1359
C
        WRITE(6,1357)
1357  FORMAT('      FOURIER TRANSFORM CHOICE NOT DEFINED.'///,
+          '      ENTER NEW CHOICE:')
        READ*, HH
C

```

```

GO TO 1356
C
1359 WRITE(1,*) HH
      WRITE(6,1370)
1370 FORMAT(/'ENTER ETA (L/RAMMDA). ( DEFAULT = 12.0D-2 ) ' )
      READ*, ETA
      IF(ETA.GT.0.0) GOTO 1385
      ETA=12.0D0
1385 WRITE(1,*) ETA
      WRITE(6,1400)
1400 FORMAT(/'ENTER THE MAXIMUM VALUE OF THETA TO BE',
+          ' CALCULATED(DEG).'/ ' ( DEFAULT = 45.0 ' )
      READ*, TMAX
      IF(TMAX.GT.0.0) GOTO 1415
      TMAX=45.0D0
1415 WRITE(1,*) TMAX
      WRITE(6,1430)
1430 FORMAT(/'ENTER THE ANGLE CALCULATION INCREMENT(DEG)',
+          '(DEFAULT=0.1) ' )
      READ*, DT
      IF(DT.GT.0.0) GOTO 1445
      DT=0.10D0
1445 WRITE(1,*) DT
      WRITE(6,1460)
1460 FORMAT(/'ENTER THE ANGLE MARKING INCREMENT(DEG)',
+          '(DEFAULT=15.0) ' )
      READ*, SDXX
      IF(SDXX.GT.0.0) GOTO 1475
      SDXX=15.0D0
1475 WRITE(1,*) SDXX
      WRITE(6,1490)
C1490 FORMAT(/'ENTER THE BEAM ENERGY (MEV) (DEFAULT=100.0) ' )
1490 FORMAT(/'ENTER THE VALUE OF NBETA (DEFAULT=0.98) ' )
C      READ*, E
      READ*, NBETA
C      IF(E.GT.0.0) GOTO 1505
      IF(NBETA.GT.0.0) GOTO 1505
C      E=100.0D0
      E=0.98D0
C1505 WRITE(1,*) E
1505 WRITE(1,*) NBETA
      WRITE(6,1520)
1520 FORMAT(/'ENTER THE HARMONIC NUMBER (DEFAULT=1.0) ' )
      READ*, N
      IF(N.GT.0.0) GOTO 1535
      N=1.0D0
1535 WRITE(1,*) N
C
      IF (HH.NE.1) GOTO 1575
C
      WRITE(6,1550)
1550 FORMAT(/'ENTER THE BUNCH LENGTH (M).( DEFAULT = 0.24D-2 ) ' )

```

```

      READ*, B
C
      IF(B.GT.0.0) GOTO 1565
C
      B=0.24D0
1565  WRITE(1,*) B
C
1575  IF ((HH.LT.2).OR.(HH.GT.4)) GOTO 1605
C
      WRITE(6,1580)
1580  FORMAT(/'ENTER THE LEVEL FUNCTION LENGTH (M).',
+        ' (DEFAULT=0.01) ' )
      READ*, LL
C
      IF(LL.GT.0.0) GOTO 1595
C
      LL=0.01D0
1595  WRITE(1,*) LL
C
1605  IF (HH.NE.3) GOTO 1635
C
      WRITE(6,1610)
1610  FORMAT(////'ENTER THE FOURIER RATIO CONSTANT (DEFAULT=1.0).')
      READ*, RR
C
      IF(RR.GT.0.0) GOTO 1625
C
      RR=1.0D0
1625  WRITE(1,*) RR
C
1635  IF (HH.NE.3) GOTO 1665
C
      WRITE(6,1640)
1640  FORMAT(/'ENTER THE NUMBER OF RIPPLES (DEFAULT=1.0) ' )
      READ*, NN
C
      IF(NN.GT.0.0) GOTO 1655
C
      NN=1.0000
1655  WRITE(1,*) NN
C
1665  IF (HH.NE.4) GOTO 1700
C
      WRITE(6,1670)
1670  FORMAT(/'ENTER NUMBER OF HUMPS (DEFAULT=2) ' )
      READ*, HU
C
      IF(HU.GT.2) GOTO 1680
C
      HU=2
1680  WRITE(1,*)HU
C

```

```

1700 IF (HH.NE.5) GOTO 1800
C
    WRITE (6,1710)
1710 FORMAT(/'ENTER THE ROUNDED FUNCTION LEVEL TOP LENGTH (CM)',
+         /'          (DEFAULT = 1.0) ' )
    READ*, RFTL
C
    IF (RFTL.GT.0.0) GOTO 1730
C
    RFTL = 1.0D0
1730 WRITE (1,*) RFTL
    WRITE (6,1760)
1760 FORMAT (/ 'ENTER THE ROUNDED FUNCTION BASE LENGTH (CM).',
+         /'          (DEFAULT = 2.0) ' )
    READ*, RFBL
C
    IF (RFBL.GT.0.0) GOTO 1780
C
    RFBL = 1.0D0
1780 WRITE (1,*) RFBL
C
1800 IF (HH.NE.6) GOTO 1900
C
    WRITE (6,1810)
1810 FORMAT (/ 'ENTER THE TRAPEZOIDAL FUNCTION LEVEL TOP',
+         /'LENGTH (CM).', /'          (DEFAULT = 1.0)' )
    READ*, TFTL
C
    IF (TFTL.GT.0.0) GOTO 1830
C
    TFTL = 1.0D0
1830 WRITE (1,*) TFTL
    WRITE (6,1860)
1860 FORMAT (/ 'ENTER THE TRAPEZOIDAL FUNCTION BASE LENGTH (CM)',
+         /'          (DEFAULT = 2.0) ' )
    READ*, TFBL
C
    IF (TFBL.GT.0.0) GOTO 1880
C
    TFBL = 1.0
1880 WRITE (1,*) TFBL
C
1900 IF (HH.NE.7) GOTO 1990
C
    WRITE (6,1910)
1910 FORMAT (/ 'ENTER TRIANGLE FUNCTION BASE LENGTH (CM).',
+         /'          (DEFAULT = 1.0) ' )
    READ*, TRIBL
C
    IF (TRIBL.GT.0.0) GOTO 1930
C
    TRIBL = 1.0D0

```

```
1930  WRITE (1,*) TRIBL  
      WRITE (6,1941)  
1941  FORMAT(/'TEST LINE THREE' )  
C  
1990  ENDFILE 1  
C  
      WRITE(6,1991) .  
1991  FORMAT(/'TEST LINE FOUR' )  
      RETURN  
      END  
C
```

APPENDIX B

PROGRAM FOR PLOTTING THE RADIATION PATTERN

```

*****
* THIS PROGRAM IS TO PLOT THE POWER PER UNIT SOLID ANGLE RADIATED *
* AT THE FREQUENCY NU. THE THEORY AND ALL EQUATIONS ARE DESCRIBED *
* IN REF.3. IT ASSUMES THETA IN COL. 1 (DEGREES) AND POWER IN COL. 2 *
* (WATT) RESPECTIVELY. IT SUPPORTS A SINGLE PLOT OF MULTIPLE CURVES *
* AND USES THE COMPRS/DISSPOP OPTION OF DISSPLA. *
*****
C
  REAL YX,XMIN,XMAX,YMIN,YMAX,X,Y,DX,AX,AY,XPHY,YPHY
  INTEGER IOUT,ITICK,ITICKX,ITICKY,IYVAR,ICT,INN,NB,NETA,NF,
+      NBL,LF,NMOD,NRAM,TLL,BL,NL
  CHARACTER*1 YES,ANS
  CHARACTER*4 BLNK(2)
  CHARACTER*60 IMESS,IPHI,IRAM,IMOD,INB,IBL,IETA,LFL,INF,ITLL,
+      INL
C
  DIMENSION X(2000),Y(2000)
  DIMENSION YX(1:5000,1:2)
C
  DATA YES/'Y'/
  DATA BLNK/' ',' '/
  EPS=.001
C
C      INITIALISE PLOTTER
C
  100 CONTINUE
  9400 FORMAT(A1)
  9401 FORMAT(I1)
  9402 FORMAT(I2)
  WRITE(4,9403)
  9403 FORMAT(' DO YOU WANT:',/,
X      ' 1. COMPRES',/,
X      ' 2. TEK618',/,
X      ' ENTER NUMBER (I1)',/)
  READ(4,*) IOUT
  IF(IOUT.EQ.1) THEN
    CALL COMPRS
  ELSEIF(IOUT.EQ.2) THEN
    CALL TEK618
  ENDIF
  AX = 4.6810
  AY = 6.7416

```

```

CALL HWROT('MOVIE')
CALL PAGE(8.5,11.0)
XPHY=2.0840
YPHY=2.7953
C
C  DEFINE: LOWER/UPPER CASE STD AND GREEK SHIFT LABELS (+,!,?,%),
C  SHIFT FOR INSTRUCTION SET(&), AND THE TYPE FACE.
C
CALL MX1ALF('STANDARD','!')
CALL MX2ALF('L/CSTD','+')
CALL MX3ALF('GREEK','?')
CALL MX4ALF('L/CGREEK','%')
CALL MX5ALF('INSTRU','&')
CALL SWISSL
CALL SHDCHR(90.,1,0.002,1)
9410 FORMAT(D16.8)
CALL HEIGHT(0.14)
CALL PHYSOR(XPHY,YPHY)
CALL AREA2D(AX,AY)
C
C      CLOSE GRAPH AND REOPEN FOR LABEL AXES NUMBER TYPES
C
CALL ENDGR(0)
CALL PHYSOR(XPHY,YPHY)
CALL AREA2D(AX,AY)
CALL XNONUM
C
C      DETERMINE THE AXIS LABELS:
C
C      X-AXIS LABEL AND NUMBER TYPE
C
CALL EXCMS('CLRSCRN')
WRITE(4,9415)
9415 FORMAT(' DO YOU WANT INTEGERS ON THE X-AXIS? (Y/N)',/)
READ(4,9400) ANS
IF(ANS.EQ.YES) CALL XINTAX
CALL XNAME('A+NGLE! (?Q!, +DEGREES!)$',100)
C
C      Y-AXIS LABEL AND NUMBER TYPE
C
WRITE(4,9417)
9417 FORMAT(' CHOOSE THE Y VARIABLE TO BE PLOTTED (I1):',/,
X      '          1 ----- W (WATT) ',/,
X      '          2 ----- DJ      ',/)
READ(4,*) IYVAR
IF (IYVAR.EQ.2) THEN
CALL YNAME('D+J      !$',100)
ELSE
CALL YNAME('W (W+ATT!)$',100)
ENDIF
C
C  ROTATE NUMBERS ON Y-AXIS AND REVERSE TICKS

```

```

C
CALL YAXANG(0.)
CALL XREVTK
CALL YREVTK
WRITE(4,7900)
7900 FORMAT(' INPUT YMIN OF THE FIRST SUBPLOT (F16.8):',/)
READ(4,*) YMIN
CALL YAXEND('NOLAST')
YMAX=YMIN+.1
CALL GRAF(0.,1.,1.,YMIN,YMAX,.1)
CALL THKFRM(.027)
CALL FRAME
CALL ENDGR(0)

```

```

C
C      CLOSED GRAF FOR AXIS LABELS, NOW REOPEN TO PLOT
C

```

```

CALL PHYSOR(XPHY,YPHY)
CALL AREA2D(AX,AY)
CALL RESET('YAXEND')
CALL RESET('XNONUM')
CALL YNAME(BLNK,2)
CALL XNAME(BLNK,2)
CALL ENDGR(0)

```

```

C
C      POSITION OR REPOSITION ORIGIN AND SCALE PLOT
C

```

```

CALL PHYSOR(XPHY,YPHY)
CALL AREA2D(AX,AY)
CALL RESET('YAXEND')
CALL YAXEND('NOFIRST')

```

```

C
C      DEFINE COORDINATE SYSTEM
C      KEEP OR CHANGE CONSTANTS
C

```

```

CALL EXCMS('CLRSCRN')
WRITE(4,9423)
9423 FORMAT(' INPUT XMIN: (F16.8)')
READ(4,*) XMIN
WRITE(4,9424)
9424 FORMAT(' INPUT XSTEP: (F16.8)')
READ(4,*) XSTEP
WRITE(4,9425)
9425 FORMAT(' INPUT XMAX: (F16.8)')
READ(4,*) XMAX
WRITE(4,9427)
9427 FORMAT(' INPUT YMIN: (F16.8)')
READ(4,*) YMIN
WRITE(4,9426)
9426 FORMAT(' INPUT YSTEP: (F16.8)')
READ(4,*) YSTEP
WRITE(4,9429)
9429 FORMAT(' INPUT YMAX: (F16.8)')

```

```

      READ(4,*) YMAX
      CALL EXCMS('CLRSCRN')
      WRITE(4,9330)
9330  FORMAT(' HOW MANY TICKS PER X-AXIS STEP? (I2)')
      READ(4,*) ITICKX
      CALL XTICKS(ITICKX)
      WRITE(4,9331)
9331  FORMAT(' HOW MANY TICKS PER Y-AXIS STEP? (I2)')
      READ(4,*) ITICKY
      CALL YTICKS(ITICKY)
      IF(XSTEP.EQ.0.0) XSTEP=(XMAX-XMIN)/AX
      IF(YSTEP.EQ.0.0) YSTEP=(YMAX-YMIN)/AY
      CALL GRAF(XMIN,XSTEP,XMAX,YMIN,YPEST,YMAX)
      CALL YNONUM
      CALL YGRAXS(YMIN,YPEST,YMAX,AY,' $',-100,AX,0.0)
      CALL RESET ('YNONUM')
      CALL XNONUM
      CALL XGRAXS(XMIN,XSTEP,XMAX,AX,' $',-100,0.0,AY)
      CALL RESET ('XNONUM')

C
C      CURVE PLOTTING
C
      CALL LINESP(1.8)
      CALL SPLINE
      CALL THKCRV(0.02)
      CALL GRACE (0.00)

C
C      DRAW A CONNECTED CURVE
C
C      MULTIPLE CURVE RETURN POINT
2000  CONTINUE
      CALL EXCMS('CLRSCRN')
      WRITE(4,9445)
9445  FORMAT(' YOU HAVE A CHOICE OF LINE TYPE:',/,
+      ' 1 ----- SOLID LINE',/,
+      ' 2 ----- DOTTED LINE',/,
+      ' 3 ----- DASHED LINE',/,
+      ' 4 ----- CHAIN DOT LINE',/,
+      ' 5 ----- CHAIN DASH LINE',/,
+      ' PLEASE INPUT LINE TYPE NUMBER: (I1)',/)
      READ(4,*) ICT
      IF(ICT.EQ.2) CALL DOT
      IF(ICT.EQ.3) CALL DASH
      IF(ICT.EQ.4) CALL CHNDOT
      IF(ICT.EQ.5) CALL CHNDSH
      CALL EXCMS('CLRSCRN')

C
C      DATA INPUT FROM EXTERNAL DATA FILE
C
      WRITE(4,9455)
9455  FORMAT(' INPUT THE FILE DATA SET NUMBER (I2)')
      READ(4,*) INN

```

```

      NUCOLS = 2
      IN=0
      DO 2400 II=1,5000
        READ(INN,9460) (YX(II,JJ),JJ=1,NUCOLS)
9460    FORMAT(4X,F8.3,2X,F20.18)
        IF((YX(II,1) .LE. 0.0).AND.(II.GT.2)) GO TO 8000
        IN=IN+1
2400    CONTINUE
8000    CONTINUE
        ICOL = 2
        DO 8010 II=1,IN
          X(II)=YX(II,1)
          Y(II)=YX(II,ICOL)
8010    CONTINUE
        REWIND INN

C
C      TERMINATE DATA READING & PLOT CURVE
C
      CALL CURVE(X,Y,IN,0)

C
C      RESET LINE TYPE
C
      IF(ICT.EQ.2) CALL RESET('DOT')
      IF(ICT.EQ.3) CALL RESET('DASH')
      IF(ICT.EQ.4) CALL RESET('CHNDOT')
      IF(ICT.EQ.5) CALL RESET('CHNSH')
      CALL EXCMS('CLRSCRN')
      WRITE(4,9473)
9473    FORMAT(' DO YOU WISH TO TERMINATE THIS SUBPLOT?')
      READ(4,9400) ANS
      IF(ANS.NE.YES) GO TO 2000

C
C      END OF PLOT
C      WRITE ADDITIONAL LABELS
C
      CALL ENDGR(0)
      CALL AREA2D(AX,AY)
      CALL EXCMS('CLRSCRN')
      WRITE(4,9480)
9480    FORMAT(' DO YOU WANT ADDITIONAL LABELS ?',/)
      READ(4,9400) ANS
      IF(ANS.EQ.'N') GO TO 9900
      WRITE(4,9483)
9483    FORMAT(' YOU HAVE A CHOICE OF FUNCTION :',/,
+      '      1----- GAUSSIAN FUNCTION',/,
+      '      2----- LEVEL FUNCTION',/,
+      '      6----- TRAPEZOIDAL FUNCTION',/,
+      '      INPUT THE NUMBER OF FUNCTION TYPE (I1) :',/)
      READ (4,9401) NF
      IF (NF.EQ.1) THEN
        INF= 'GAUSSIAN FUNCTIONS'
        WRITE (4,9484)

```

```

9484      FORMAT('SPECIFY BUNCH LENGTH (F4.2):',/,
+          '      1 ----- 0.24 CM ',/,
+          '      2 ----- 0.88 CM ',/,
+          '      3 ----- 1.20 CM ',/,
+          '      4 ----- 1.76 CM ',/,
+          '      5 ----- 2.40 CM ',/,
+          '      6 ----- 2.63 CM ',/,
+          '      7 ----- 3.50 CM ',/,
+          '      8 ----- 4.38 CM ',/,
+          'INPUT THE NUMBER(I1):____',/ )
      READ(4,9401) NBL
      IF (NBL.EQ.1) THEN
          IBL= 'BL = 0.24 +CM!$'
      ELSEIF(NBL.EQ.2) THEN
          IBL= 'BL = 0.88 +CM!$'
      ELSEIF(NBL.EQ.3) THEN
          IBL= 'BL = 1.20 +CM!$'
      ELSEIF(NBL.EQ.4) THEN
          IBL= 'BL = 1.76 +CM!$'
      ELSEIF(NBL.EQ.5) THEN
          IBL= 'BL = 2.40 +CM!$'
      ELSEIF(NBL.EQ.6) THEN
          IBL= 'BL = 2.63 +CM!$'
      ELSEIF(NBL.EQ.7) THEN
          IBL= 'BL = 3.50 +CM!$'
      ELSE
          IBL= 'BL = 4.38 +CM!$'
      ENDIF
      ELSEIF(NF.EQ.2) THEN
          INF= 'LEVEL FUNCTIONS'
          WRITE(4,9486)
9486      FORMAT('SPECIFY LEVEL FUNCTION LENGTH (F4.2):',/,
+          '      1 ----- 1.00 CM ',/,
+          '      2 ----- 3.00 CM ',/,
+          '      3 ----- 4.50 CM ',/,
+          '      4 ----- 5.00 CM ',/,
+          '      5 ----- 6.00 CM ',/,
+          '      6 ----- 7.00 CM ',/,
+          '      7 ----- 8.00 CM ',/,
+          '      8 ----- 9.00 CM ',/,
+          'INPUT THE NUMBER(I1):____',/ )
      READ(4,9401) LF
      IF (LF.EQ.1) THEN
          LFL= 'LFL = 1.00 +CM!$'
      ELSEIF(LF.EQ.2) THEN
          LFL= 'LFL = 3.00 +CM!$'
      ELSEIF(LF.EQ.3) THEN
          LFL= 'LFL = 4.50 +CM!$'
      ELSEIF(LF.EQ.4) THEN
          LFL= 'LFL = 5.00 +CM!$'
      ELSEIF(LF.EQ.5) THEN
          LFL= 'LFL = 6.00 +CM!$'

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```

ELSEIF(LF.EQ.6) THEN
    LFL= 'LFL = 7.00 +CM!$'
ELSEIF(LF.EQ.7) THEN
    LFL= 'LFL = 8.00 +CM!$'
ELSE
    LFL= 'LFL = 9.00 +CM!$'
ENDIF
ELSEIF(NF.EQ.6) THEN
    INF= 'TRAPEZOIDAL FUNCTIONS'
    WRITE(4,9501)
9501  FORMAT('SPECIFY TOP LEVEL LENGTH :',/,
+      '      1 ---- 0.07 CM ',/,
+      '      2 ---- 2.94 CM ',/,
+      '      3 ---- 3.185 CM ',/,
+      '      4 ---- 4.0 CM ',/,
+      '      5 ---- 5.0 CM ',/,
+      '      6 ---- 5.04 CM ',/,
+      '      7 ---- 8.96 CM ',/,
+      '      INPUT THE NUMBER (I1):___ ',/)
    READ(4,9401) TLL
    IF (TLL.EQ.1) THEN
        ITLL= 'TFTL = 0.07 +CM!$'
    ELSEIF (TLL.EQ.2) THEN
        ITLL= 'TFTL = 2.94 +CM!$'
    ELSEIF (TLL.EQ.3) THEN
        ITLL= 'TFTL = 3.185 +CM!$'
    ELSEIF(TLL.EQ.4) THEN
        ITLL= 'TFTL = 4.0 +CM!$'
    ELSEIF(TLL.EQ.5) THEN
        ITLL= 'TFTL = 5.0 +CM!$'
    ELSEIF(TLL.EQ.6) THEN
        ITLL= 'TFTL = 5.04 +CM!$'
    ELSE
        ITLL= 'TFTL = 8.96 +CM!$'
    ENDIF
    WRITE(4,9502)
9502  FORMAT('SPECIFY BASE LENGTH :',/,
+      '      1 ---- 5.215 CM ',/,
+      '      2 ---- 7.0 CM ',/,
+      '      3 ---- 8.0 CM ',/,
+      '      4 ---- 8.96 CM ',/,
+      '      INPUT THE NUMBER (I1):___ ',/)
    READ(4,9401) BL
    IF (BL.EQ.1) THEN
        IBL= 'TFBL = 5.215 +CM!$'
    ELSEIF(BL.EQ.2) THEN
        IBL= 'TFBL = 7.0 +CM!$'
    ELSEIF(BL.EQ.3) THEN
        IBL= 'TFBL = 8.0 +CM!$'
    ELSE
        IBL= 'TFTL = 8.96 +CM!$'
    ENDIF

```

```

ENDIF
WRITE(4,9485)
9485 FORMAT(' SPECIFY RADIATION MODE (I1):',/,/,
+          '          1---- CERENKOV',/,/,
+          '          2 --- SUB-CERENKOV',/,/,
+          ' INPUT THE NUMBER:____',/ )
READ(4,9401) NMOD
IF(NMOD.EQ.1) THEN
    IMOD = 'C+ERENKOV!$'
ELSE
    IMOD = '+SUB-!C+ERENKOV!$'
ENDIF
WRITE(4,9487)
9487 FORMAT(' SPECIFY ENERGY OR NBETA (I1):',/,/,
X          ' FOR E ',/,/,
X          '          1 -- E = 2.555 MEV',/,/,
X          ' FOR NBETA',/,/,
X          '          2 --- NBETA = 0.99 NM',/,/,
X          '          3 -- NBETA = 0.98 NM',/,/,
X          '          4 -- NBETA = 0.97 NM',/,/,
X          '          5 -- NBETA = 0.96 NM',/,/,
X          '          6 -- NBETA = 0.95 NM',/,/,
X          ' INPUT THE NUMBER:____',/ )
READ(4,9401) NB
IF(NB.EQ.1) THEN
C    INB = '+N!%B! = 1.00$'
    INB = 'E = 2.555 M+E!V$'
ELSEIF(NB.EQ.2) THEN
    INB = '+N!%B! = 0.99$'
ELSEIF(NB.EQ.3) THEN
    INB = '+N!%B! = 0.98$'
ELSEIF(NB.EQ.4) THEN
    INB = '+N!%B! = 0.97$'
ELSEIF(NB.EQ.5) THEN
    INB = '+N!%B! = 0.96$'
ELSE
    INB = '+N!%B! = 0.95$'
ENDIF
CALL EXCMS('CLRSCRN')
WRITE(4,9488)
9488 FORMAT(' SPECIFY ETA (I1):',/,/,
X          '          1 -- ETA = 12 ',/,/,
X          '          2 -- ETA = 24 ',/,/,
X          '          3 -- ETA = 37 ',/,/,
X          '          4 -- ETA = 74 ',/,/,
X          ' INPUT THE NUMBER:____ ',/ )
READ(4,9401) NETA
IF(NEA.EQ.1) THEN
    IETA = '%C! = 12 $'
ELSEIF(NEA.EQ.2) THEN
    IETA = '%C! = 24 $'
ELSEIF(NEA.EQ.3) THEN

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      IETA = '%C! = 37 $'
ELSE
      IETA = '%C! = 74 $'
ENDIF
WRITE(4,9490)
9490 FORMAT(' SPECIFY BEAM PATH LENGTH (I1):',/,/,
X      '      1 -- L = 21 CM (ETA=12,N=6)',/,/,
X      '      2 -- L = 42 CM (ETA=12,N=3)',/,/,
X      '      3 -- L = 64.8 CM (ETA=37,N=6)',/,/,
X      '      4 -- L = 126.2 CM (ETA=12,N=1)',/,/,
X      '      5 -- L = 129.5 CM (ETA=37,N=3)',/,/,
X      '      INPUT THE NUMBER:____ ',/)
      READ(4,9401) NL
      IF(NL.EQ.1) THEN
            INL = 'L = 21 +CM!$'
      ELSEIF(NL.EQ.2) THEN
            INL = 'L = 42 +CM!$'
      ELSEIF(NL.EQ.3) THEN
            INL = 'L = 64.8 +CM!$'
      ELSEIF(NL.EQ.4) THEN
            INL = 'L = 126.2 +CM!$'
      ELSE
            INL = 'L = 129.5 +CM!$'
      ENDIF
      WRITE(4,9492)
9492 FORMAT(' SPECIFY WAVE LENGTH (I1):',/,/,
X      '      1 -- RAMDA = 10.52 CM (N=1)',/,/,
X      '      2 -- RAMDA = 3.50 CM (N=3)',/,/,
X      '      3 -- RAMDA = 1.75 CM (N=6)',/,/,
X      '      INPUT THE NUMBER:____ ',/)
      READ(4,9401) NRAM
      IF(NRAM.EQ.1) THEN
            IRAM = '%L! = 10.52 +CM!$'
      ELSEIF(NRAM.EQ.2) THEN
            IRAM = '%L! = 3.50 +CM!$'
      ELSE
            IRAM = '%L! = 1.75 +CM!$'
      ENDIF
C
      XMES = 2.880
      YMES = 6.130
      IMESS = IMOD
      CALL MESSAG(IMESS,100,XMES,YMES)
C
      YMES = YMES - 0.250
      IMESS = INB
      CALL MESSAG(IMESS,100,XMES,YMES)
C
      YMES = YMES - 0.250
      IMESS = IETA
      CALL MESSAG(IMESS,100,XMES,YMES)
C

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      YMES = YMES - 0.250
      IMESS = INL
      CALL MESSAG(IMESS,100,XMES,YMES)
C
      YMES = YMES - 0.250
      IMESS = IRAM
      CALL MESSAG(IMESS,100,XMES,YMES)
C
      YMES = YMES - 0.250
      IF(NF.EQ.1) THEN
        IMESS=IBL
      ELSEIF(NF.EQ.2) THEN
        IMESS=LFL
      ELSEIF(NF.EQ.6) THEN
        IMESS= ITLL
        CALL MESSAG(IMESS,100,XMES,YMES)
        YMES = YMES-0.250
        IMESS = IBL
      ENDIF
      CALL MESSAG(IMESS,100,XMES,YMES)
C
      IF(HH.EQ.6) THEN
        XMES = 1.20
      ELSE
        XMES = 1.50
      ENDIF
      YMES = -2.25
      IMESS = INF
      CALL MESSAG(IMESS,100,XMES,YMES)
C
9900  CONTINUE
      CALL EXCMS('CLRSCRN')
      IF( IOUT.EQ.2) THEN
        WRITE(4,9493)
9493  FORMAT(' <CLEAR>, THEN READY FOR HARD COPY')
      ENDIF
      CALL ENDPL(0)
      WRITE(4,9495)
9495  FORMAT(' DO YOU WANT TO MAKE ANOTHER FIGURE?',/)
      READ(4,9400) ANS
      IF(ANS.NE.YES) THEN
        GO TO 9999
      ELSE
      ENDIF
      CALL RESET('ALL')
      GO TO 100

9999  CONTINUE
      CALL DONEPL
      STOP
      END

```

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